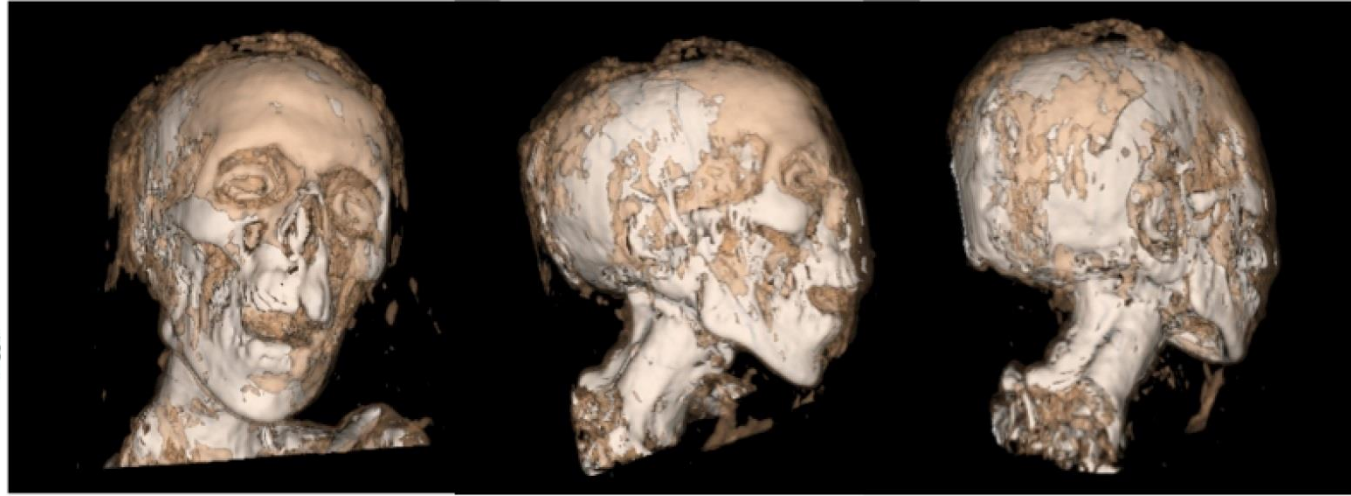
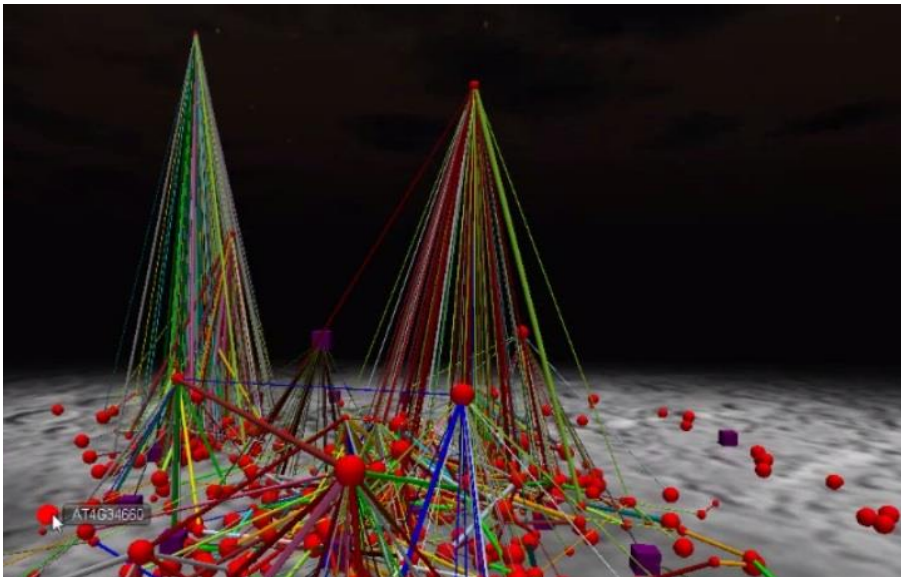


[blogs.library.duke.edu](http://blogs.library.duke.edu)

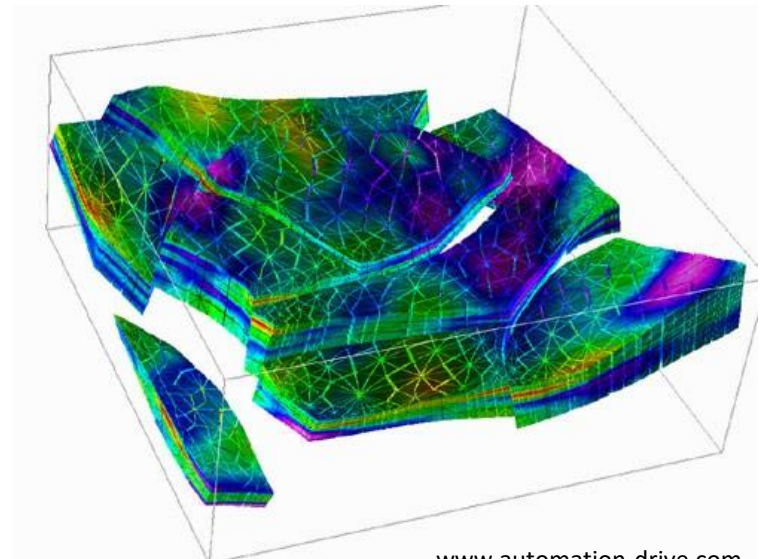


[visthis.blogspot.com](http://visthis.blogspot.com)

## 4. Spatial data visualization



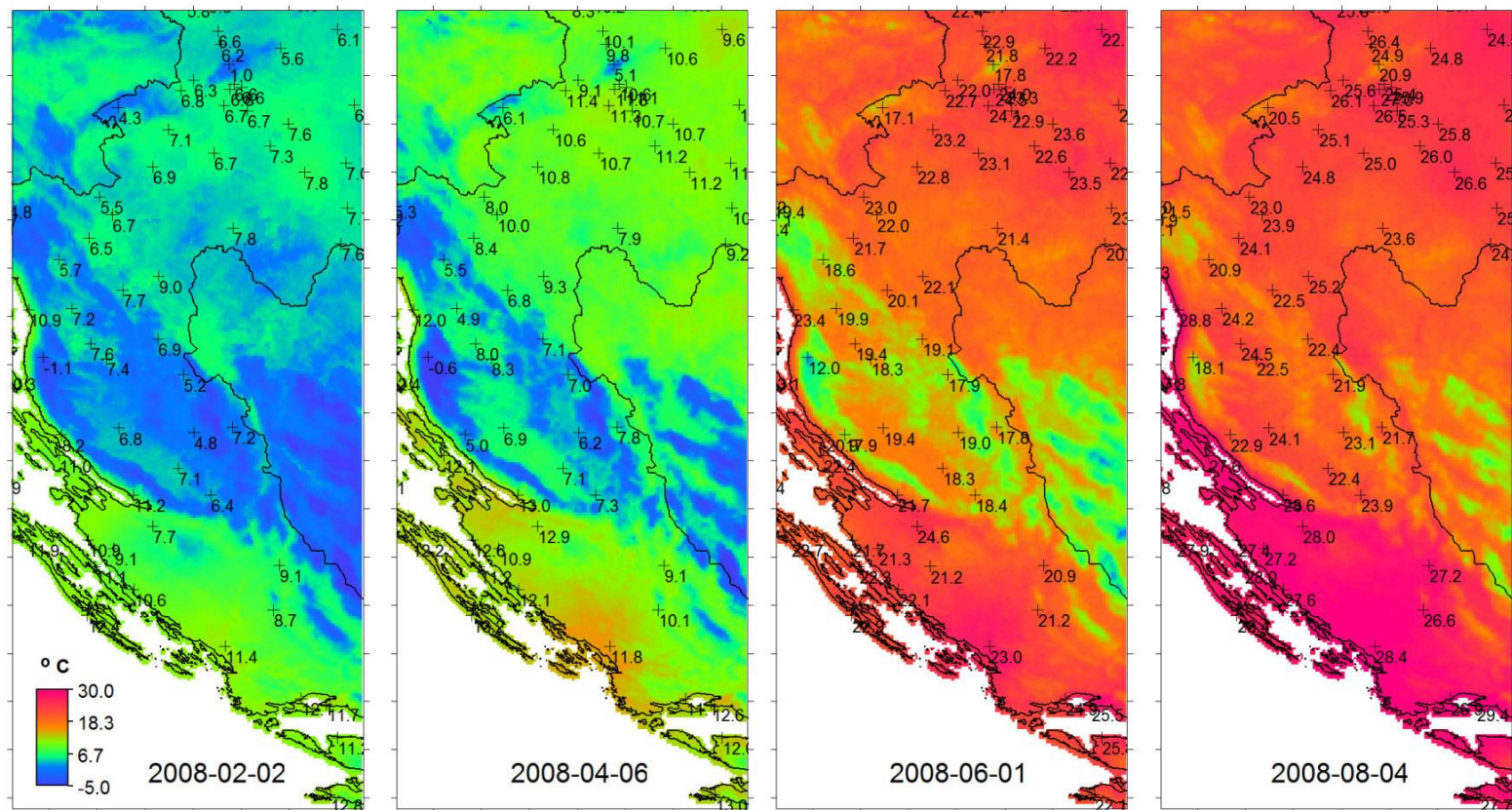
[www.hypergridbusiness.com](http://www.hypergridbusiness.com)



[www.automation-drive.com](http://www.automation-drive.com)

# Spatial data visualization

- Input data contains spatial or spatio-temporal attributes



# Real world vs. screen

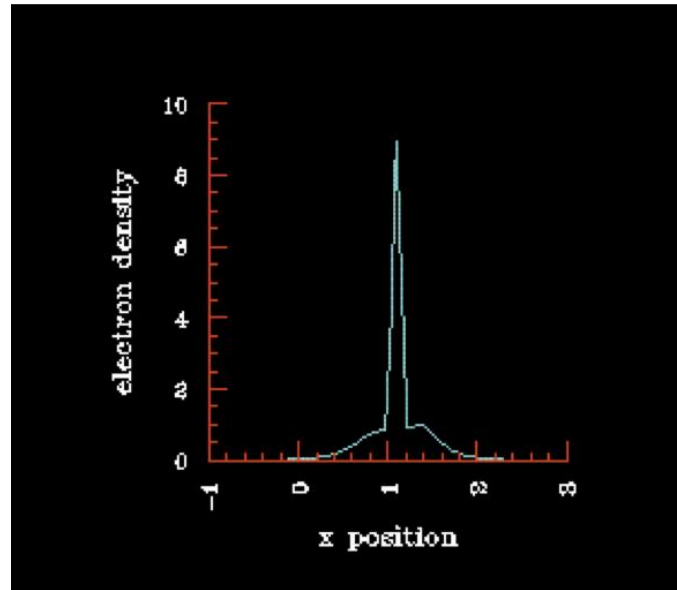
- In real world, we are not limited by 2D space, discrete representation, low resolution
- On screen:
  - Exploring data in different scales
  - Dynamic changes of contrast, lighting, resolution
  - Interactive exploration of space inaccessible in real world
  - Interactive adding and removing parts of the data

# Mapping of attributes

- Phase no. 1:
  - Mapping of spatial attributes of data to spatial attributes of the screen (transformation)
- Phase no. 2:
  - Mapping of the remaining attributes – color, texture, size, shape of graphical entities, ...

# 1D data

- Sequence of 1D data with one variable
  - Graph



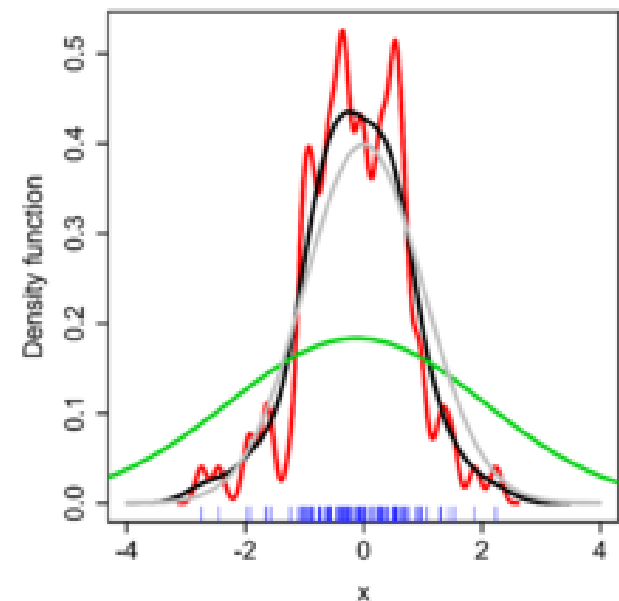
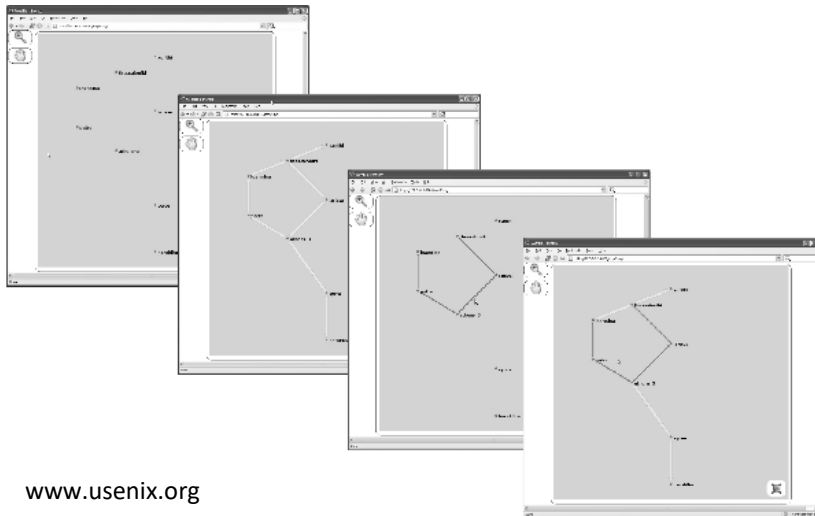
<http://www.opendx.org>

- Color bar



# 1D multivariate data

- More variables or more values for one data input
- Extension of the previous technique
  - Juxtapositioning
  - Superimpositioning

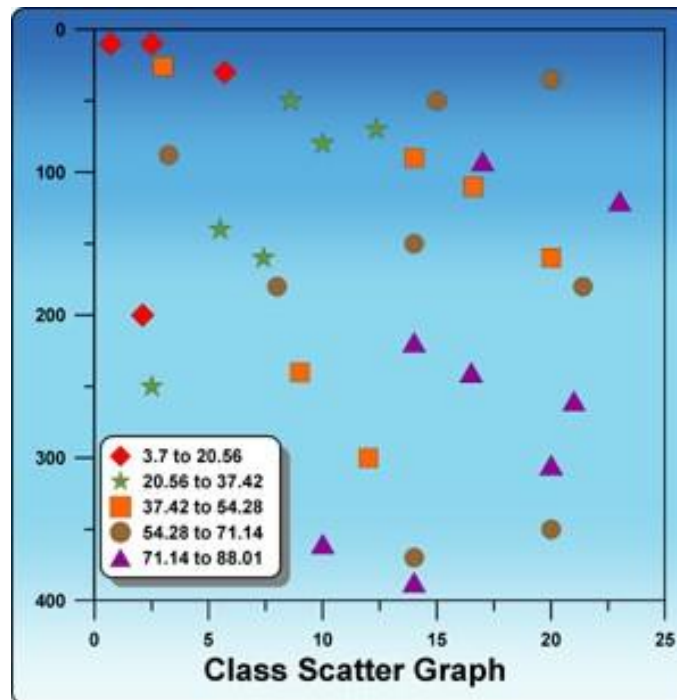


# 2D data

- Two spatial dimensions – mapping of spatial data attributes to screen space attributes
- Typical visualizations of 2D data:
  - Scatterplot
  - Map
  - Image
  - Cityscape
  - Contours, isobars

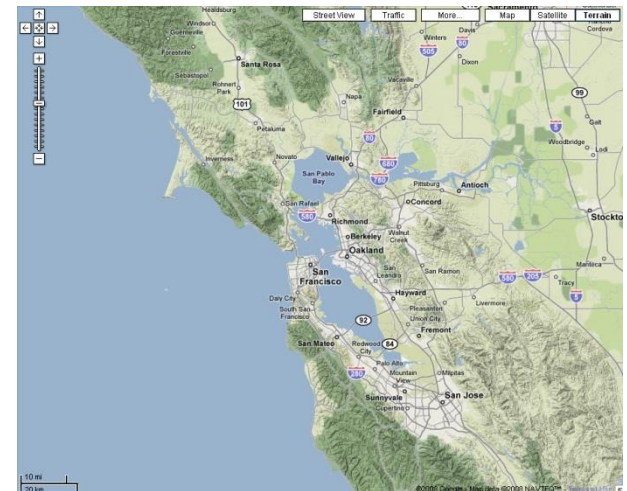
# Scatterplot

- Each data item influences color, shape, and size of the selected glyph
- No interpolation



# Map

- Linear objects – continuous line segments (rivers, roads)
- Planar objects – closed polygons with color, texture, ... (lakes, countries)
- Point objects – specific symbols (school, church)
- Labels



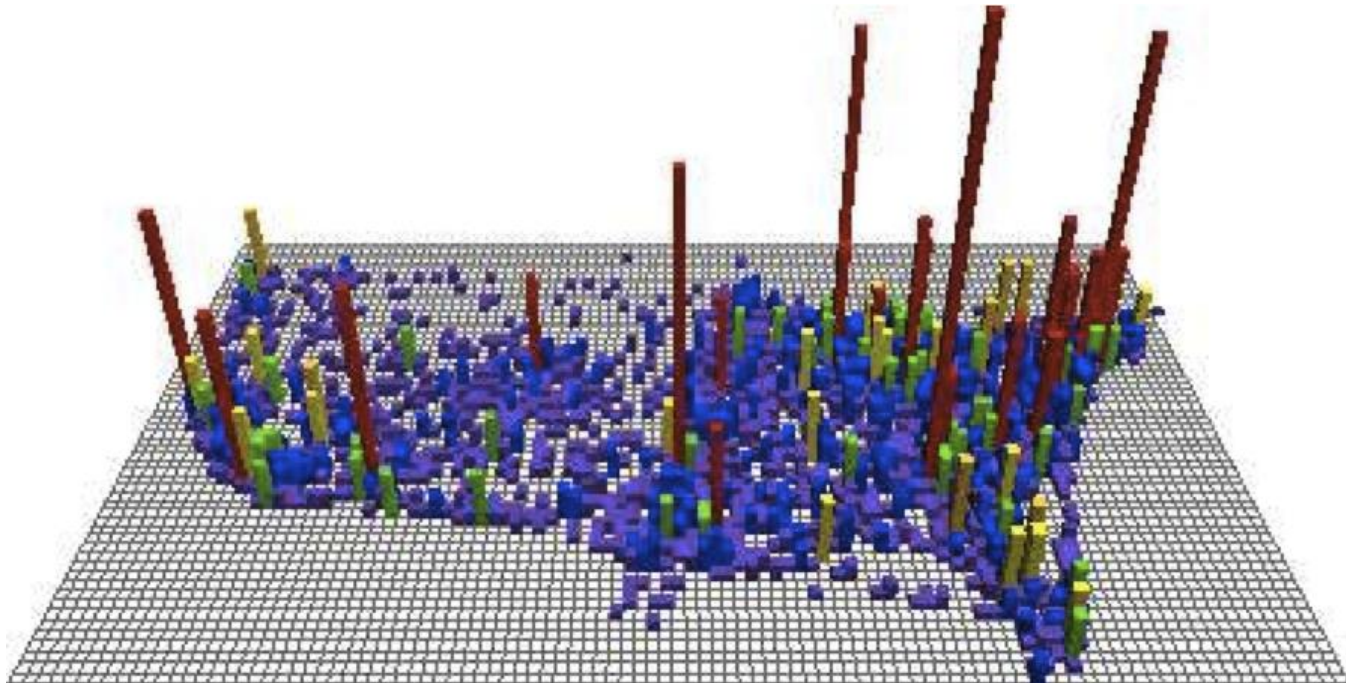
# Image

- Data value mapped onto color in given position, color between pixels has to be interpolated



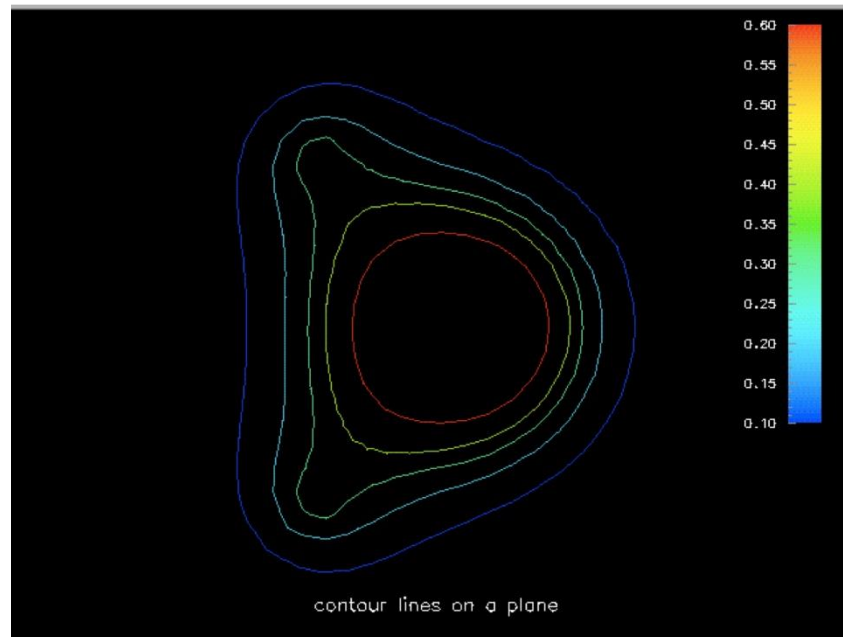
# Cityscape

- Drawing 3D blocks in plane, data mapped onto their attributes (height, color, ...)



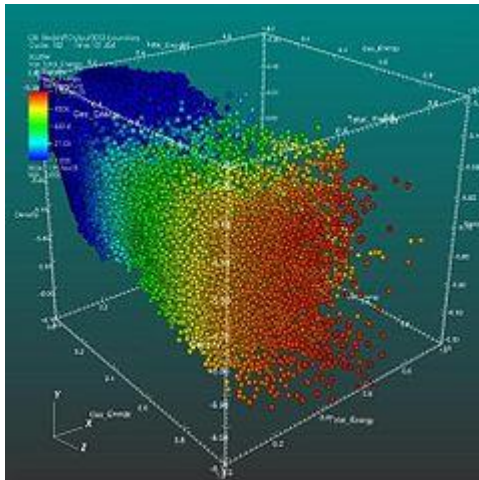
# Contours, isobars

- Border information representing a continuous phenomenon (elevation, temperature)
- Determines the boundary between points with higher and lower values

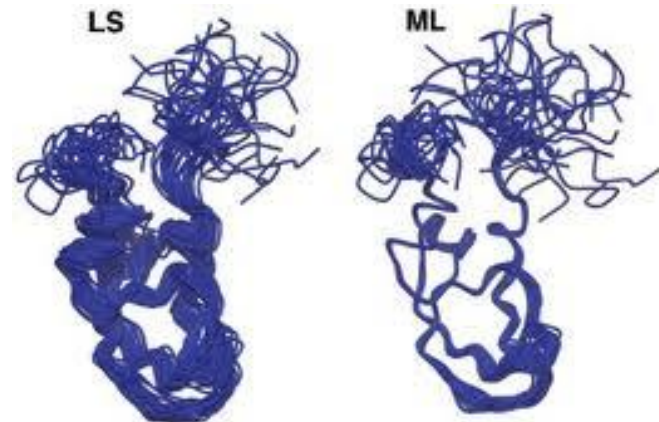


# 2D multivariate data

- Juxtapositioning
  - Stacking of 2D visualizations to 3D
- Superimpositioning
  - Overlapping 2D visualizations
- Both limited by the number of variables



en.wikipedia.org



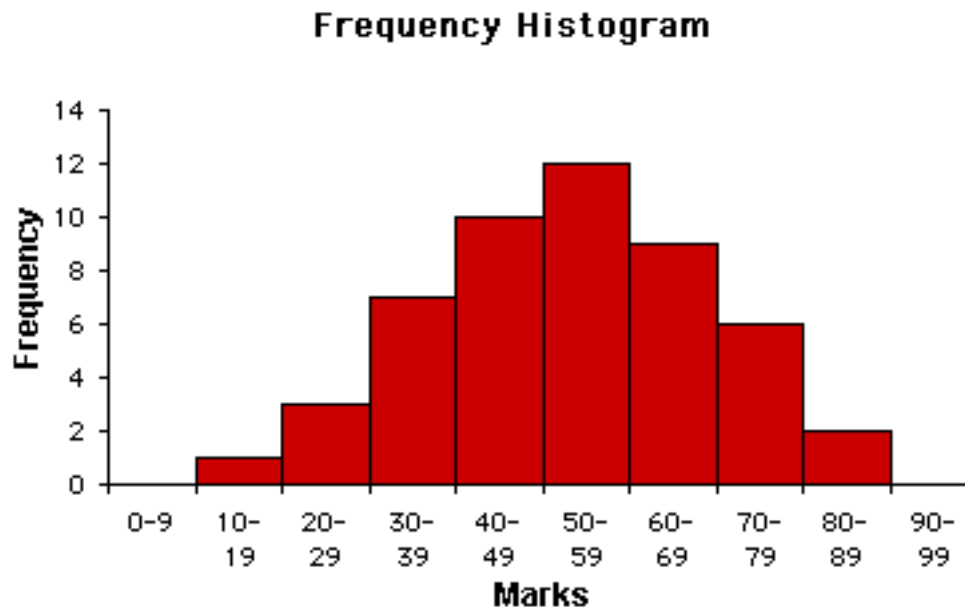
boscoh.com

# Studying 2D data

- Simplification of input data – visualization of subsets of the data, projections, summarizations
- Then using previous techniques
- Projection techniques:
  - Frequency histograms
  - Merging rows and columns
  - Linear „probes“

# Frequency histograms

- Calculating the frequency in which given values are appearing in the data
- Result is displayed as bar chart



# Merging rows and columns

- Localization of regions of interest with high or low variability
- Merging by adding, averaging, calculating median, standard deviation, maximum, minimum
- Color bars, line charts, bar charts

# Linear „probes“

- Line (ray probe) passing through the input data
- Using parametric equations and bilinear interpolation
- Defined by two points  $P_1$  and  $P_2$  or by one point and direction vector
- Parametric equation for line:

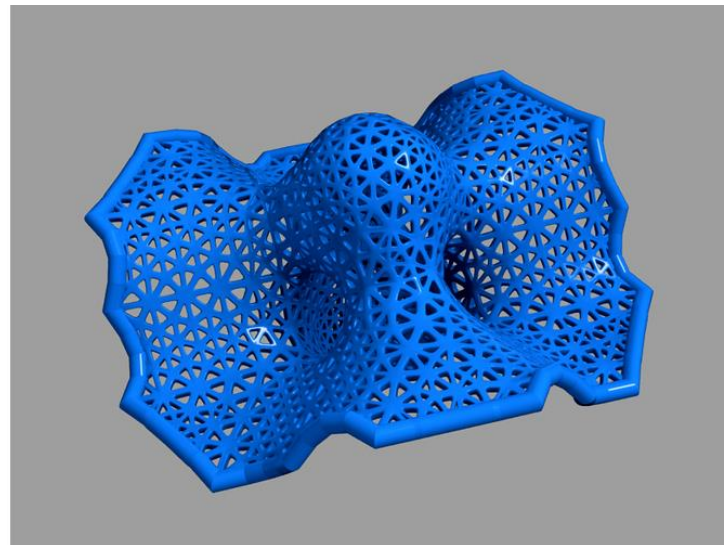
$$P(t) = P_1 + t(P_2 - P_1), \text{ where } 0 \leq t \leq 1.0$$

# 3D data

- Discrete samples of a continuous phenomenon or set of vertices, edges, and polygons
- Mostly combination of both
- Basic techniques:
  - Visualization of explicit surfaces
  - Volumetric visualization
  - Implicit surfaces

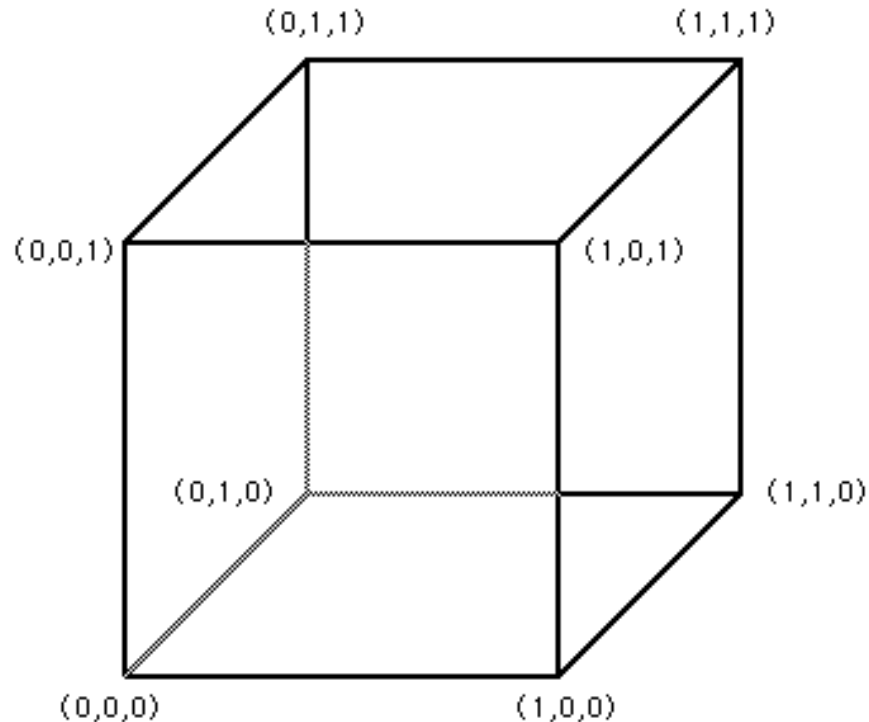
# Visualization of explicit surfaces

- Explicit surface defined as:
  - List of 3D vertices, edges, planar polygons
  - Set of parametric equations defining  $x$ ,  $y$ ,  $z$  coordinates of points, along with strategy for their connection (edges, polygons)



# Example

vertex[0] = (0., 0., 0.)  
vertex[1] = (0., 0., 1.)  
vertex[2] = (0., 1., 1.)  
vertex[3] = (0., 1., 0.)  
vertex[4] = (1., 0., 0.)  
vertex[5] = (1., 0., 1.)  
vertex[6] = (1., 1., 1.)  
vertex[7] = (1., 1., 0.)  
edge[0] = (0, 1)  
edge[1] = (1, 2)  
edge[2] = (2, 3)  
edge[3] = (3, 0)  
edge[4] = (0, 4)  
edge[5] = (1, 5)  
edge[6] = (2, 6)  
edge[7] = (3, 7)  
edge[8] = (4, 5)  
edge[9] = (5, 6)  
edge[10] = (6, 7)  
edge[11] = (7, 4)  
face[0] = (0, 1, 2, 3)  
face[1] = (8, 9, 10, 11)  
face[2] = (0, 5, 8, 4)  
face[3] = (1, 6, 9, 5)  
face[4] = (2, 7, 10, 6)  
face[5] = (3, 4, 11, 7)



# Example – unit cylinder in y axis

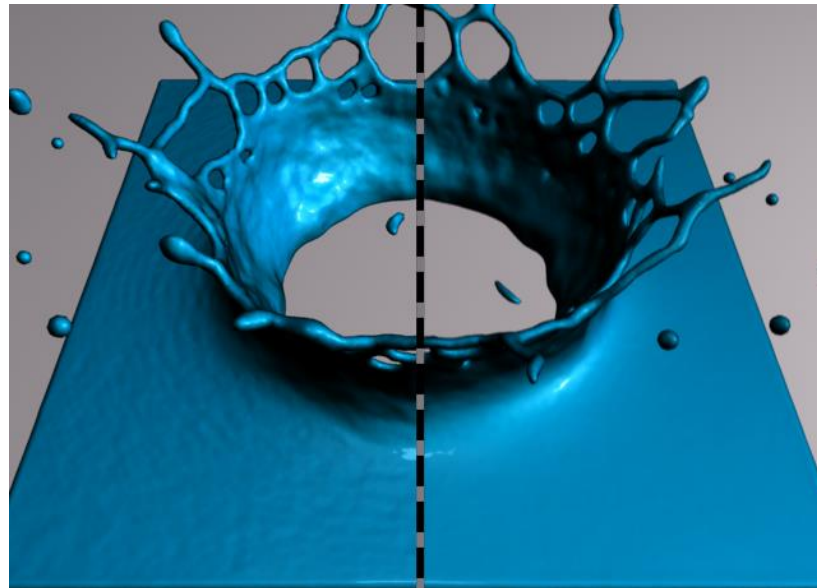
$$\begin{aligned} y = 1.0, \quad x = \cos \Theta, \quad z = \sin \Theta, \\ 0.0 \leq \Theta \leq 2\pi \end{aligned} \quad (\text{top base})$$

$$\begin{aligned} y = 0.0, \quad x = \cos \Theta, \quad z = \sin \Theta, \\ 0.0 \leq \Theta \leq 2\pi \end{aligned} \quad (\text{bottom base})$$

$$\begin{aligned} y = h, \quad x = \cos \Theta, \quad z = \sin \Theta, \\ 0.0 \leq \Theta \leq 2\pi, \quad 0.0 \leq h \leq 1.0 \end{aligned} \quad (\text{middle part})$$

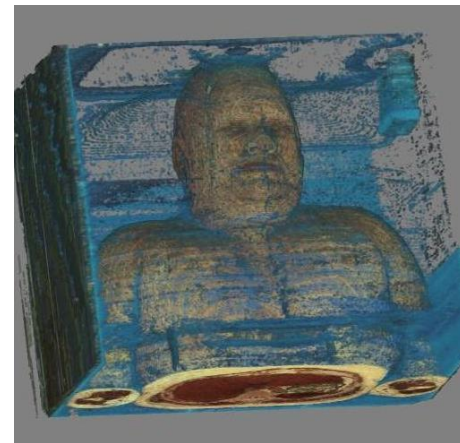
# Examples

- Input data associated with:
  - vertices – temperature, weight of vertex
  - edges – strength of chemical bond
  - polygons – map coverage of area

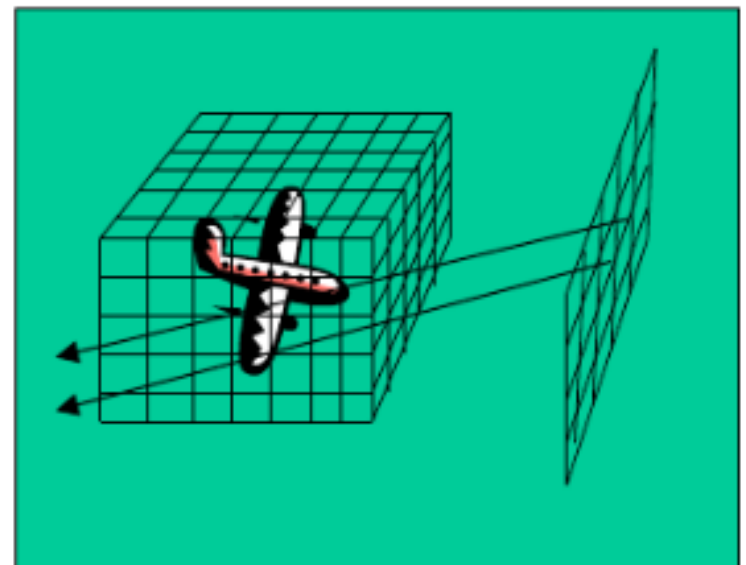


# Volumetric visualization

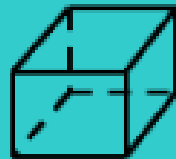
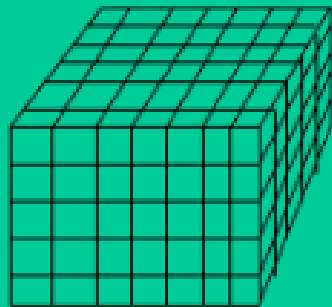
- Using voxels
- Categories:
  - Slicing – using clipping plane
  - Isosurfaces – generating surface
  - Direct volume rendering – ray casting or projecting of voxels to projection plane



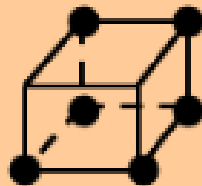
[vidi.cs.ucdavis.edu](http://vidi.cs.ucdavis.edu)



# Voxel



A voxel is a cubic cell, which has a single value cover the entire cubic region



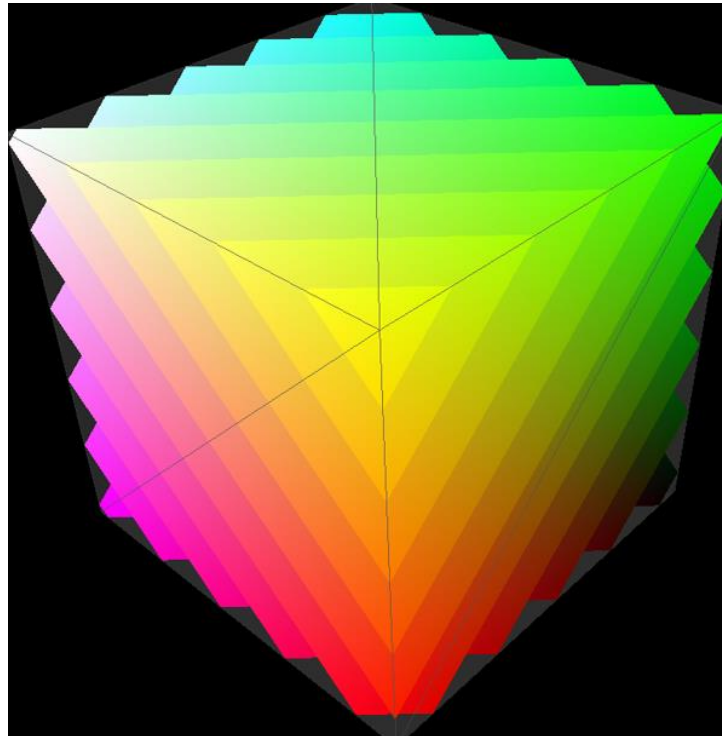
A voxel is a data point at a corner of the cubic cell  
The value of a point inside the cell is determined by interpolation

# Resampling

- Important for most of the volumetric visualization techniques
  - Isosurfaces
  - Slicing
  - Direct volume rendering

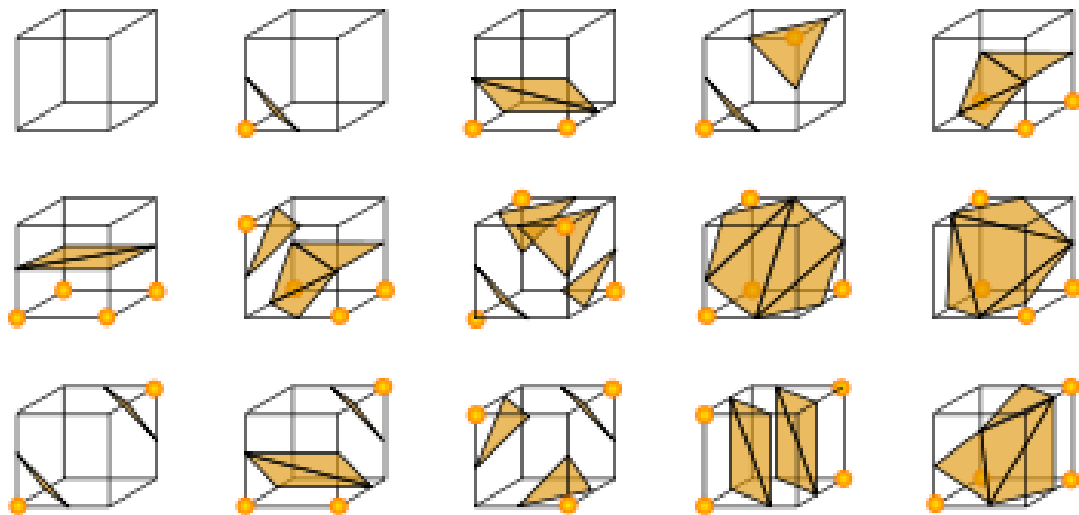
# Slicing of volumetric data using clip planes

- Creates a subset of input data in lower dimension



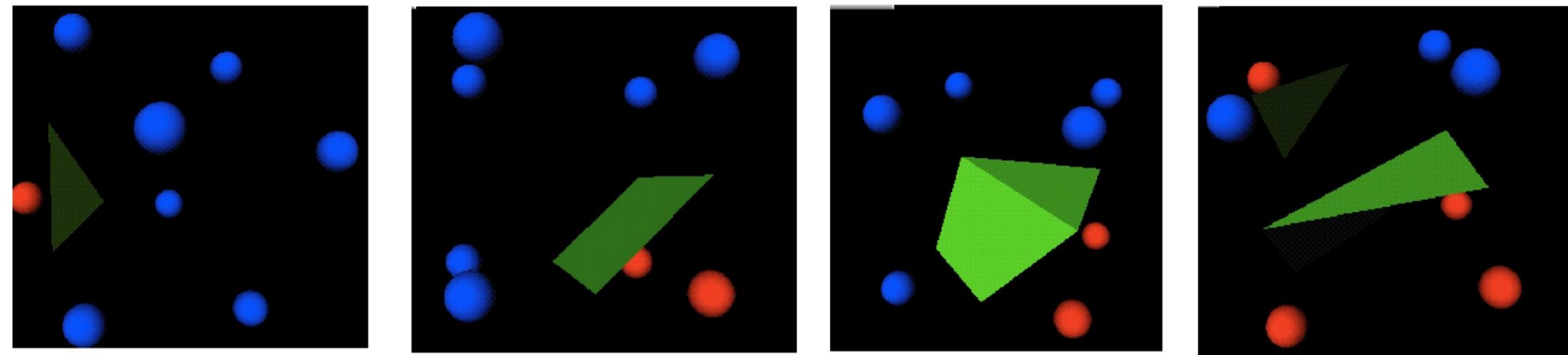
# Generating isosurface using Marching Cubes

- Lorensen, Cline (1987)
- Voxel = cube with vertices
- Algorithm creates triangles based on the correspondence between vertices and isosurface

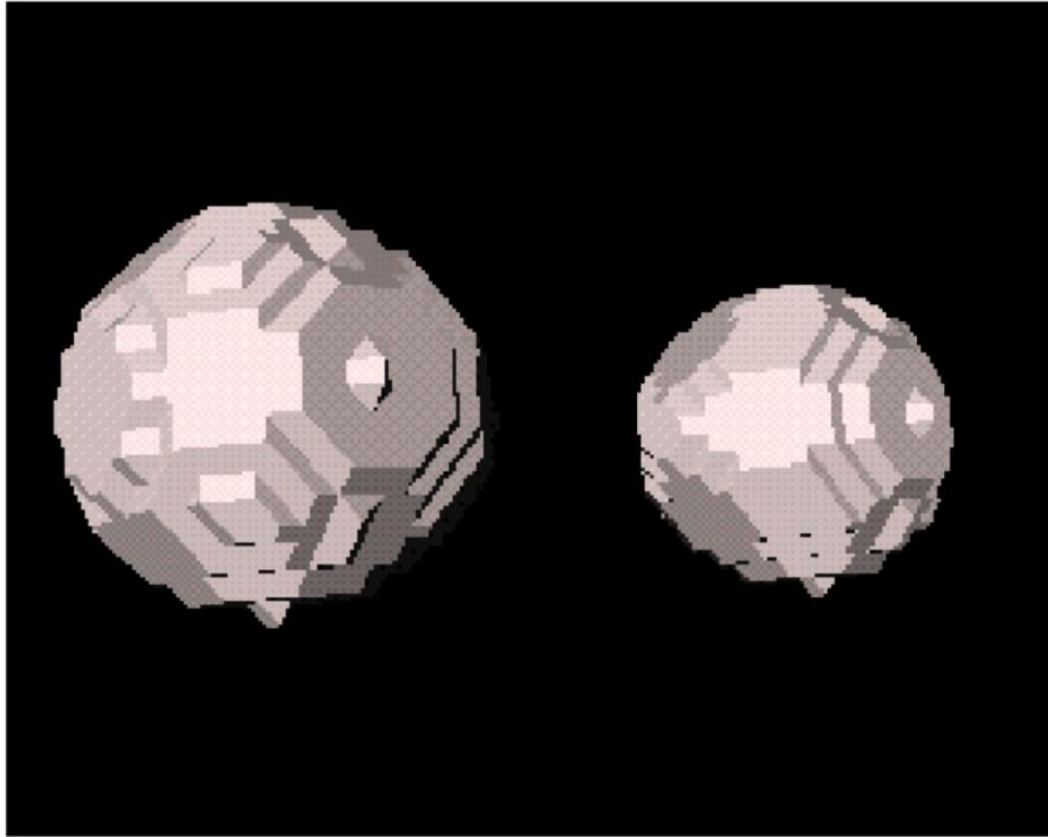


# Marching Cubes – details

- 256 configurations, thanks to symmetry only 16 unique (1 = whole cube inside, 1 = whole cube outside)
- Generating corresponding triangles



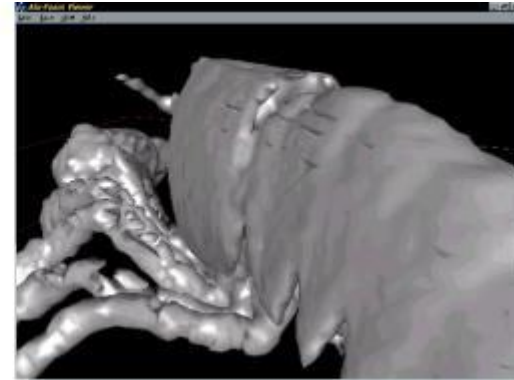
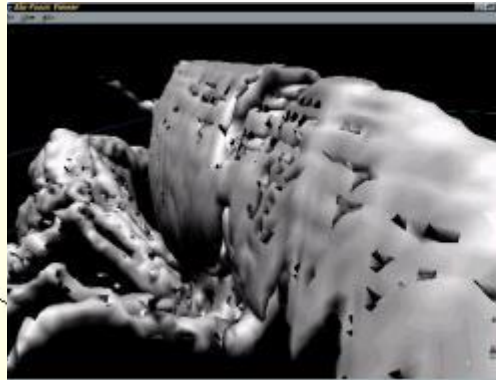
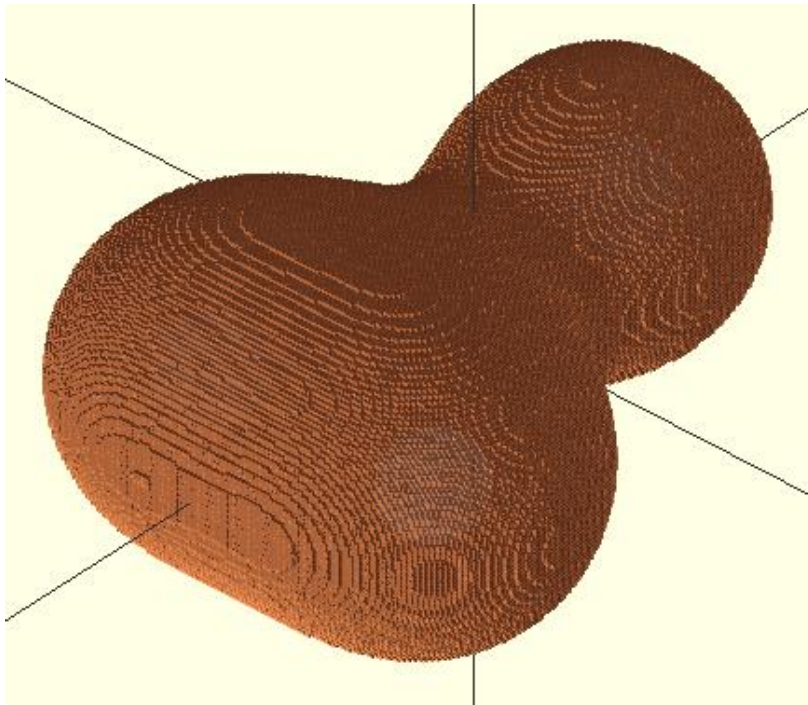
# Marching Cubes - details



(<http://www.opendx.org>)

# Marching Cubes - problems

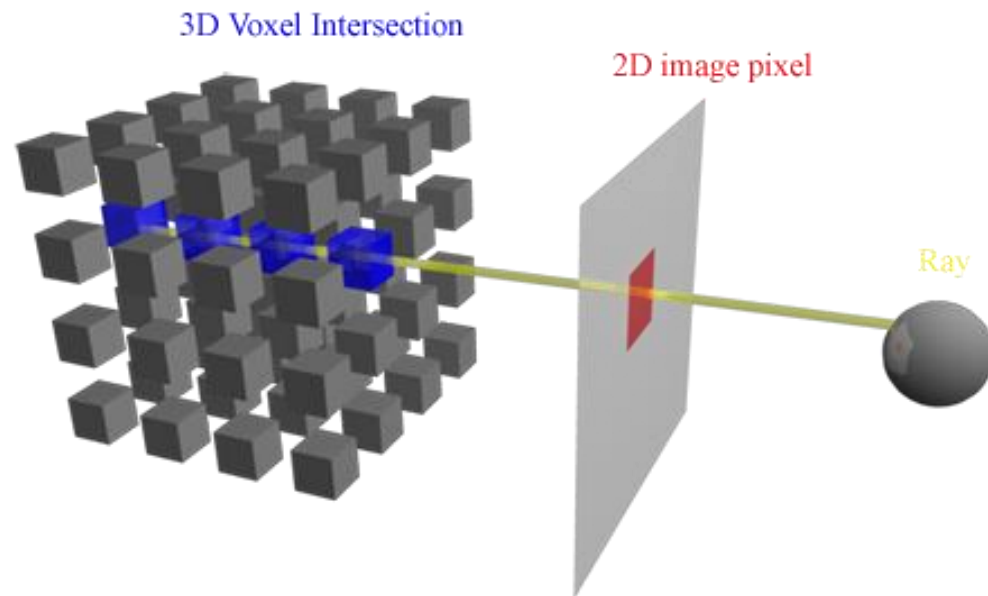
- High memory requirements
- Holes in data – poor quality of input data



[www.cescg.org](http://www.cescg.org)

# Direct volume visualization

- Pixels of the resulting image computed individually – using ray casting or voxel projection
- Methods:
  - Forward mapping
  - Inverse mapping (ray casting)



# Forward mapping - problems

- F1: How to deal with pixels which are influenced by more voxels?
- F2: How to deal with pixels without any voxels mapped onto them?
- F3: How to deal with situation when voxels are projected to positions between pixels?

# Inverse mapping - problems

- I1: How to choose correct number of points along ray which will be sampled?
- I2: How to calculate the value in these points if they hit the space between voxels?
- I3: How to combine points hit by the ray?

# Solution

- F2 and F3: Mapping of each voxel to a region of the projection plane. Each voxel then partially influences values of several neighboring pixels
- I1: Determining the spacing between pixels and setting the sampling frequency to the smaller value than this spacing

# Solution

- F1 and I3: Compositing
  - Each voxel has associated the transparency value
  - Voxel  $i$  has color  $c_i$  and transparency  $o_i$ , then its contribution to the resulting pixel value is:

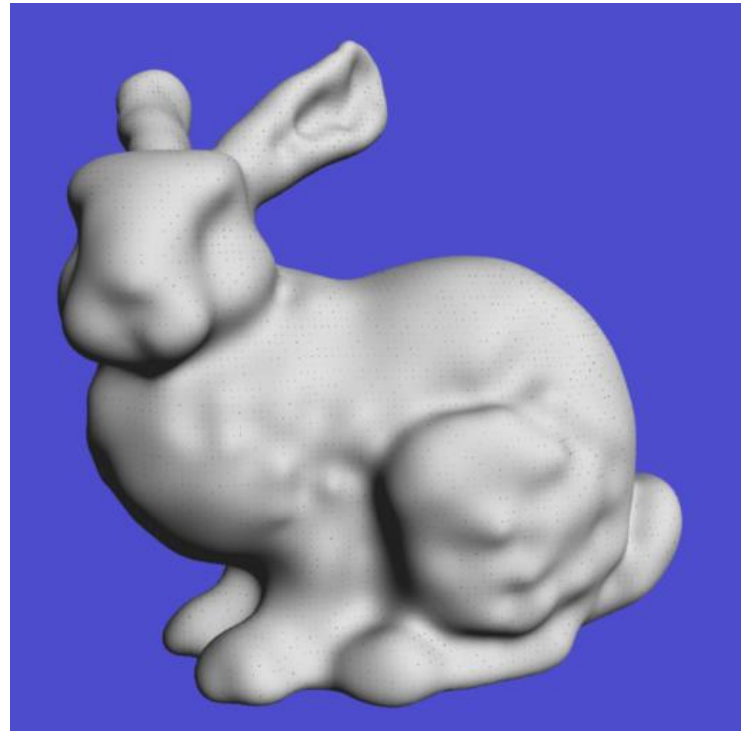
$$c_i * o_i * \prod_{j=0}^{i-1} (1 - o_j)$$

- Resulting pixel value is then determined as:

$$I(x, y) = \sum_{i=0}^n c_i * o_i * \prod_{j=0}^{i-1} (1 - o_j)$$

# Implicit surfaces

- Surface is defined as zero contour for function with two or three variables



# Dynamic data

- Flow visualization – methods for visualizing the dynamic behavior of fluids



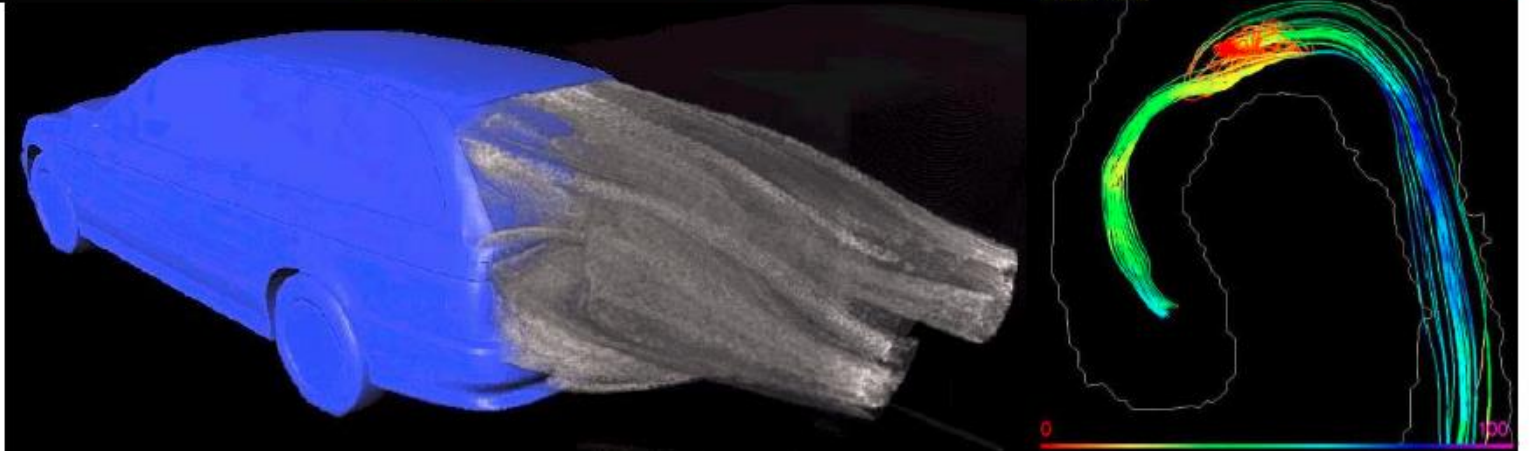
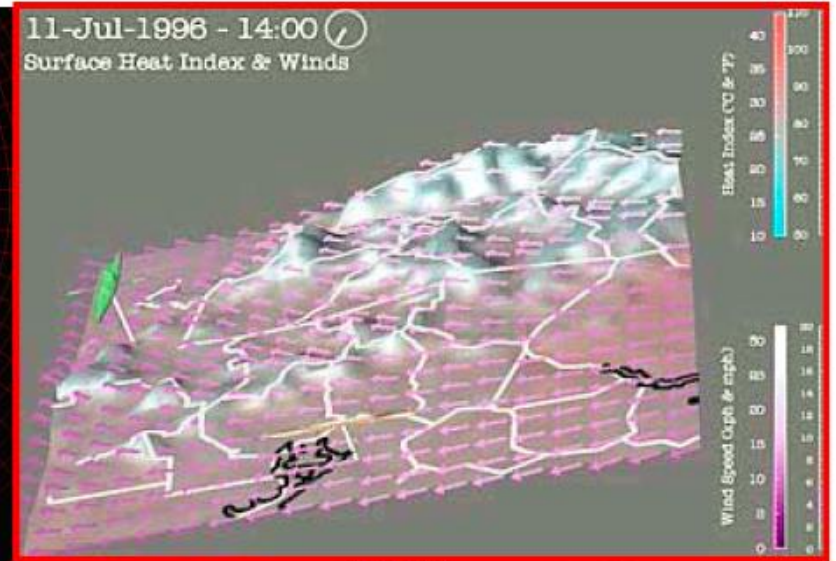
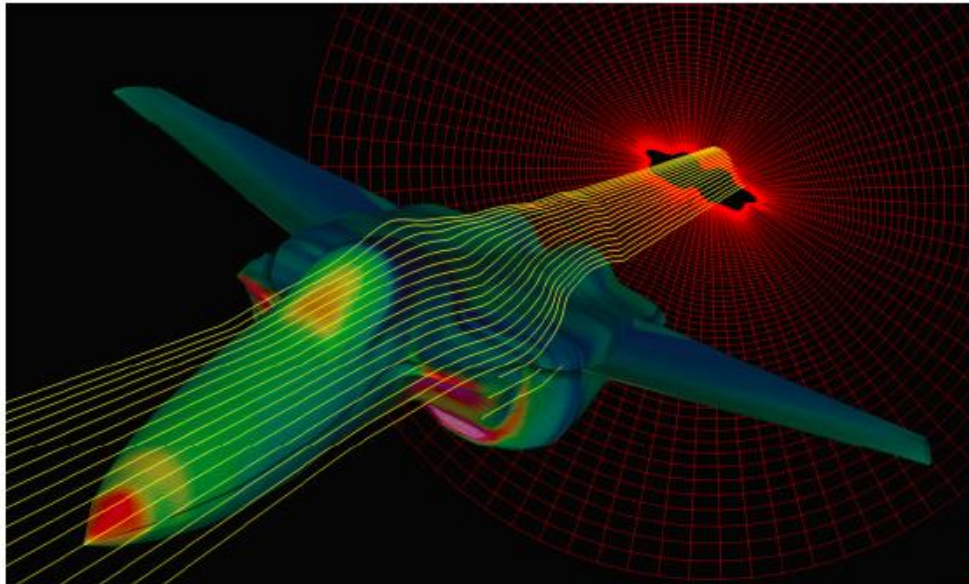
# Flow visualization

- Visualization of changes
- Typically more than 3D
- User goals
  - Data overview vs. details
- Input data:
  - Simulation – flight, ship, car industry, weather forecast, medicine (blood flow), ...
  - Measurements – wind tunnel (aerodynamics)
  - Models – using differential equations

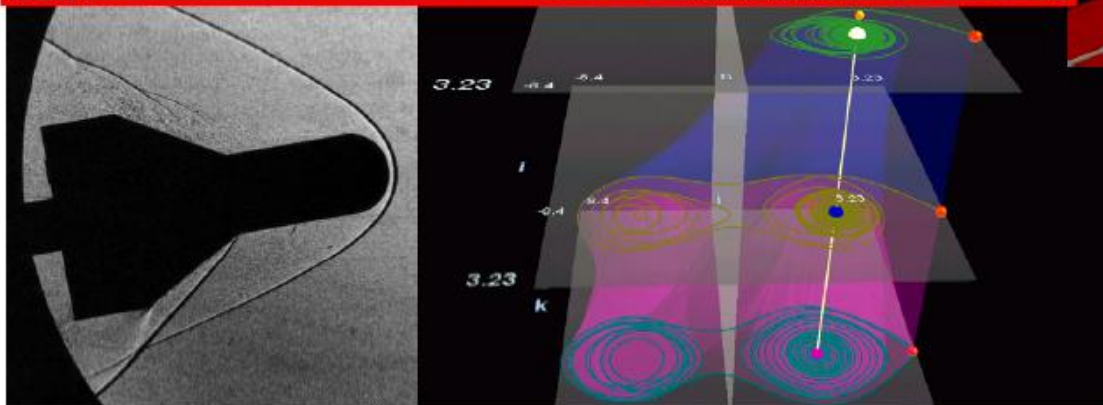
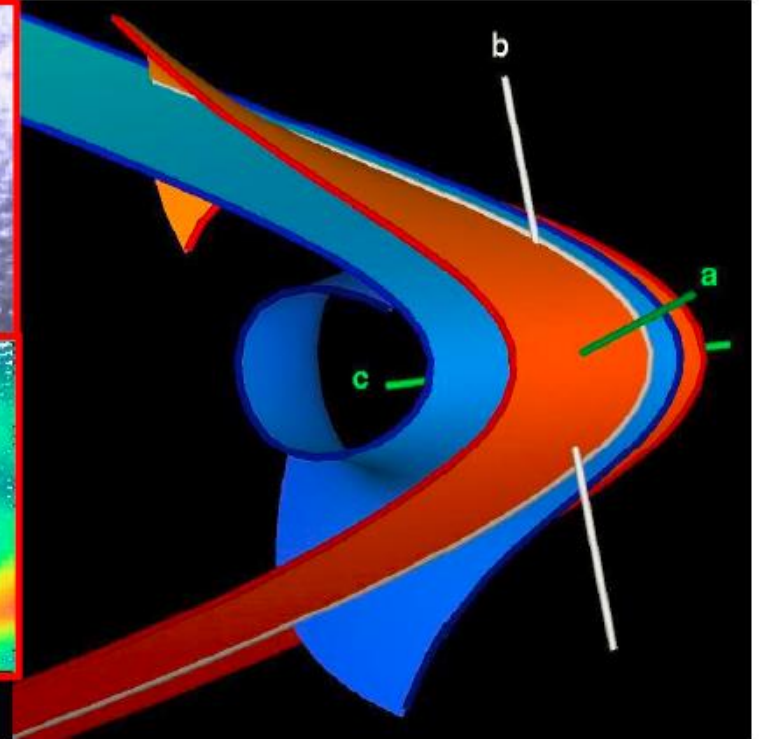
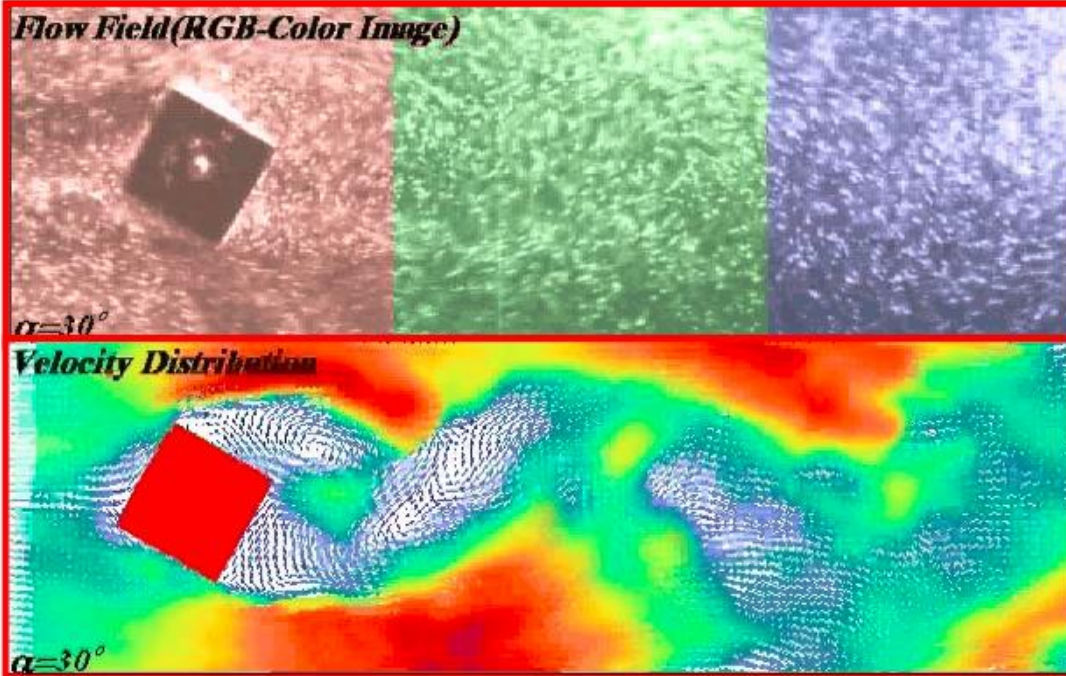


<http://en.wikipedia.org/wiki/File:Windkanal.jpg>

# Examples

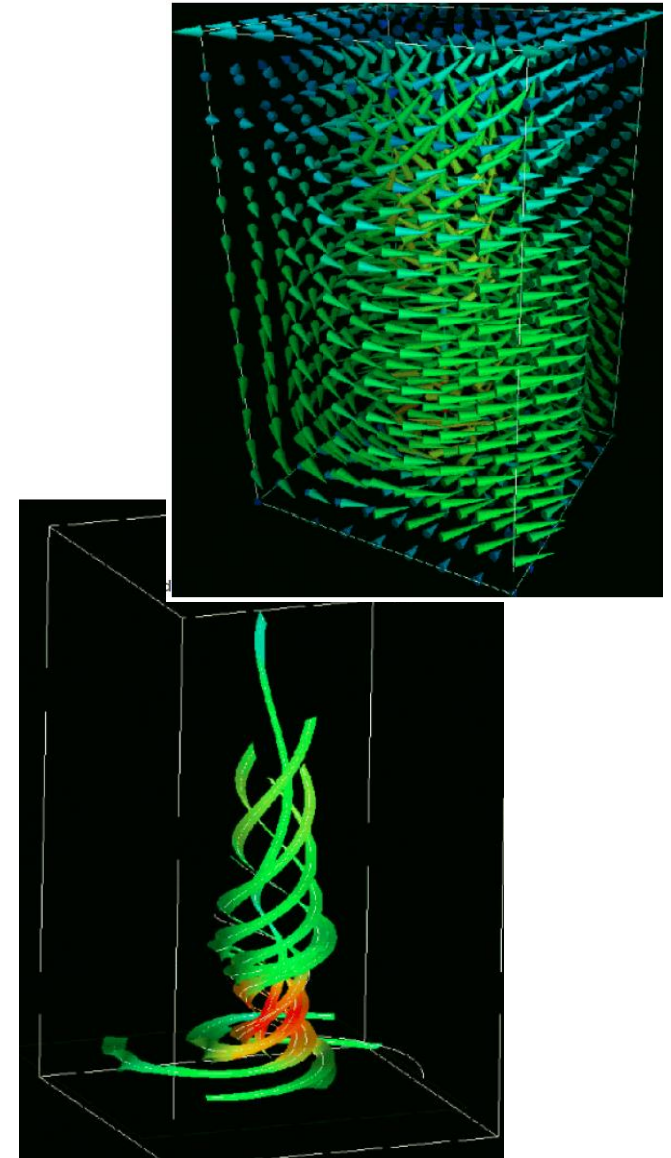


# Examples



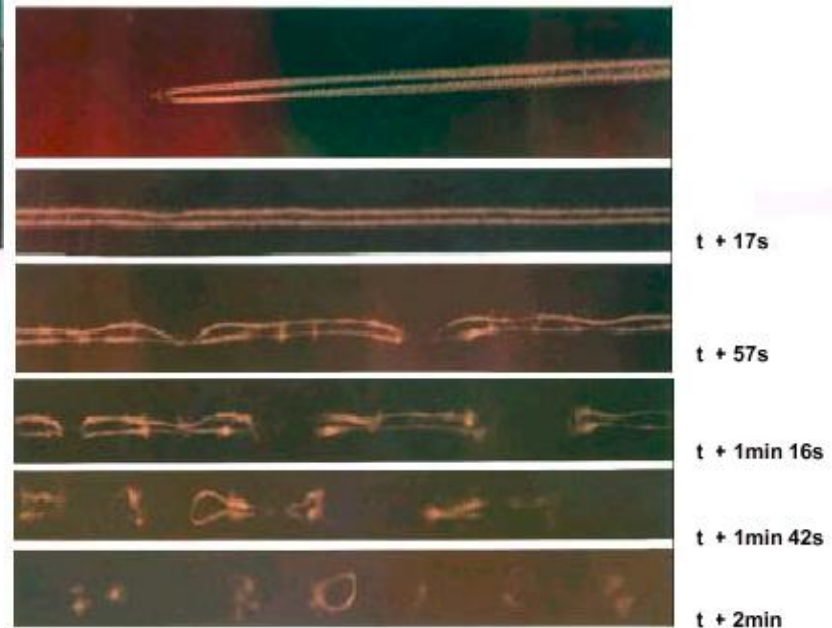
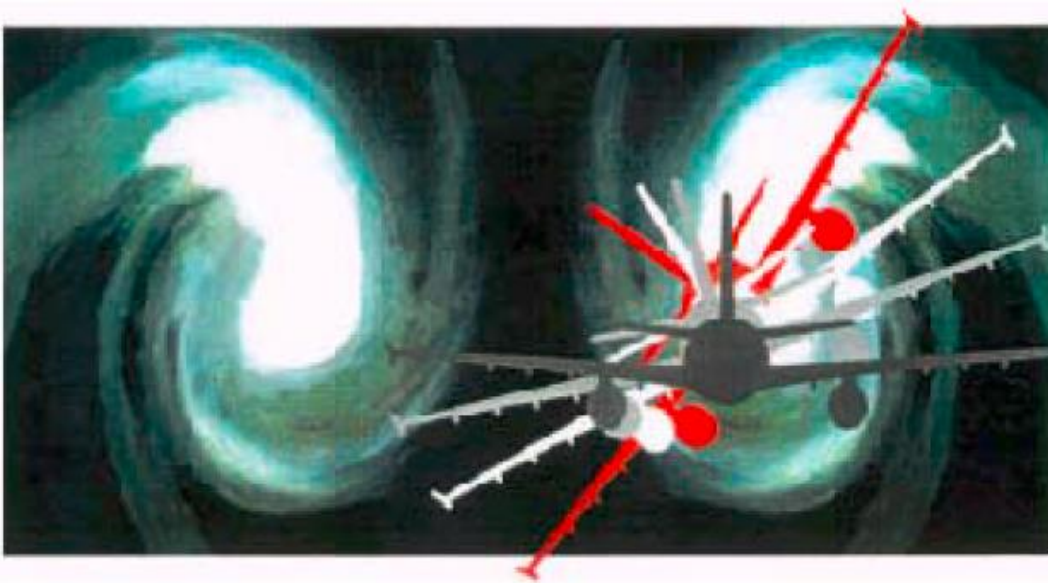
# Direct vs. Indirect flow visualization

- Direct
  - View onto the current state of the flow
  - Vector field visualization
- Indirect
  - Visualizing the evolution of flow over time
  - Streamlines, streamsurfaces



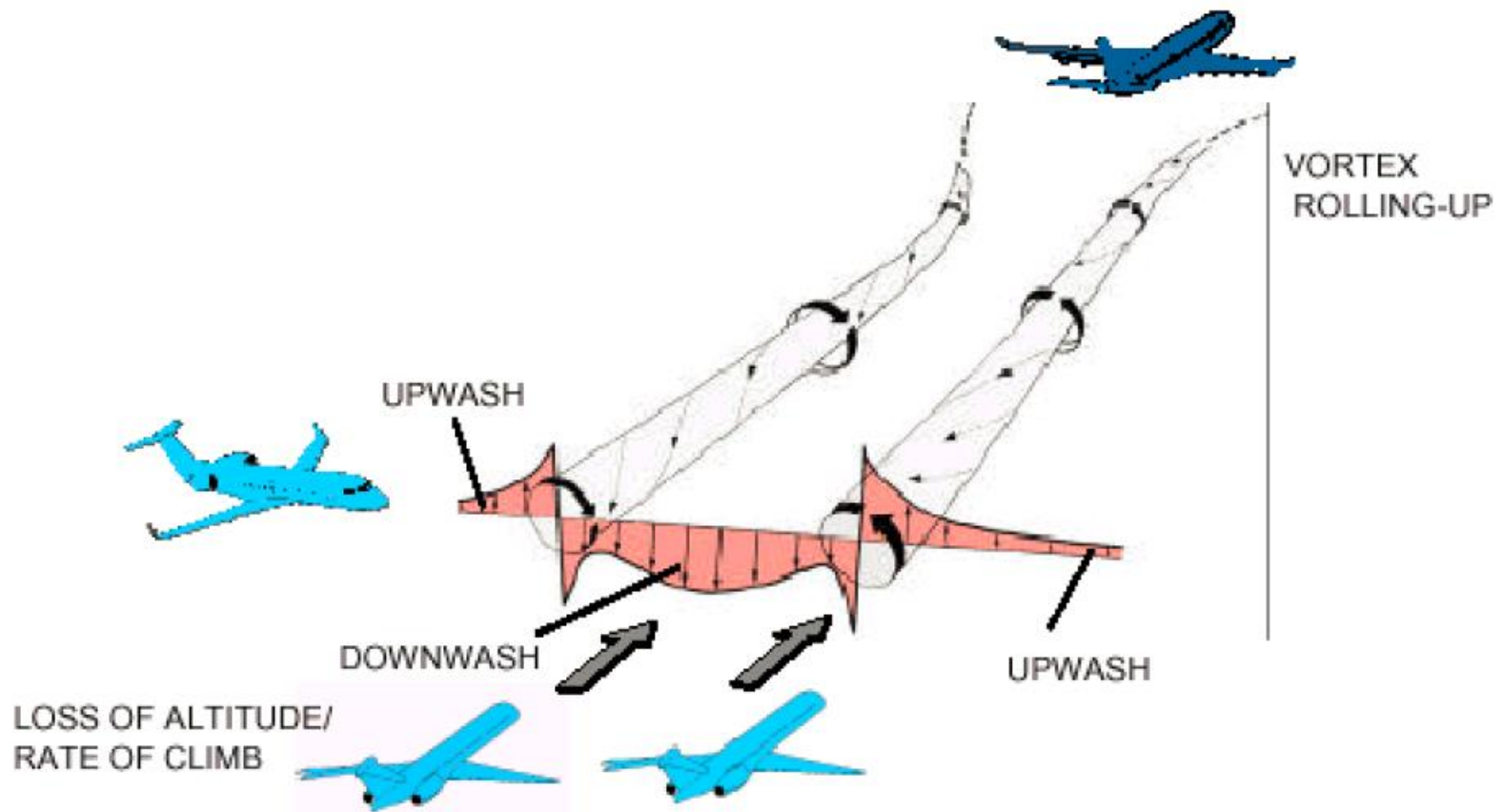
# Example – Wind-Tip vortex

- Problem: turbulence behind plane



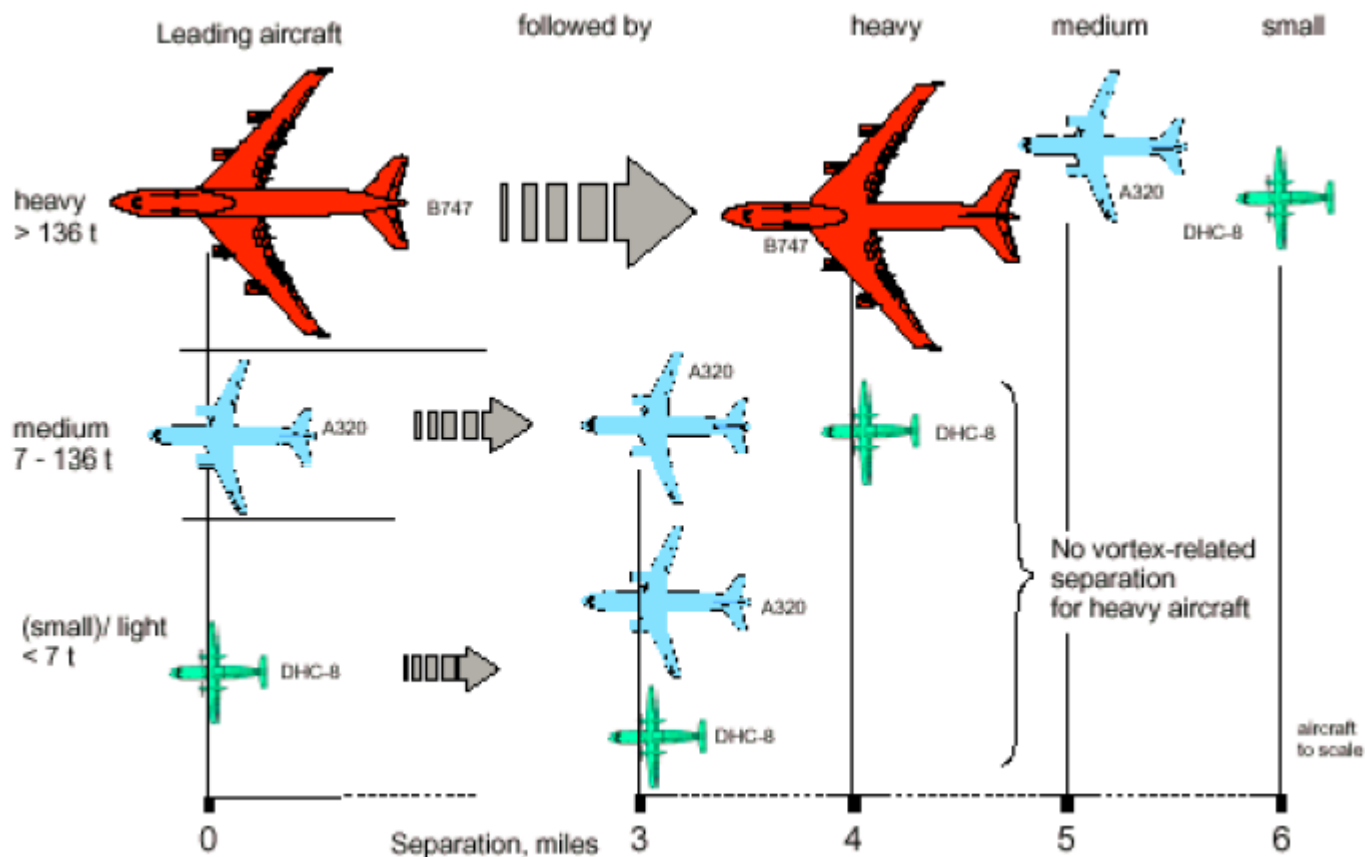
# Example – Wind-Tip vortex

- Vortex can be dangerous!



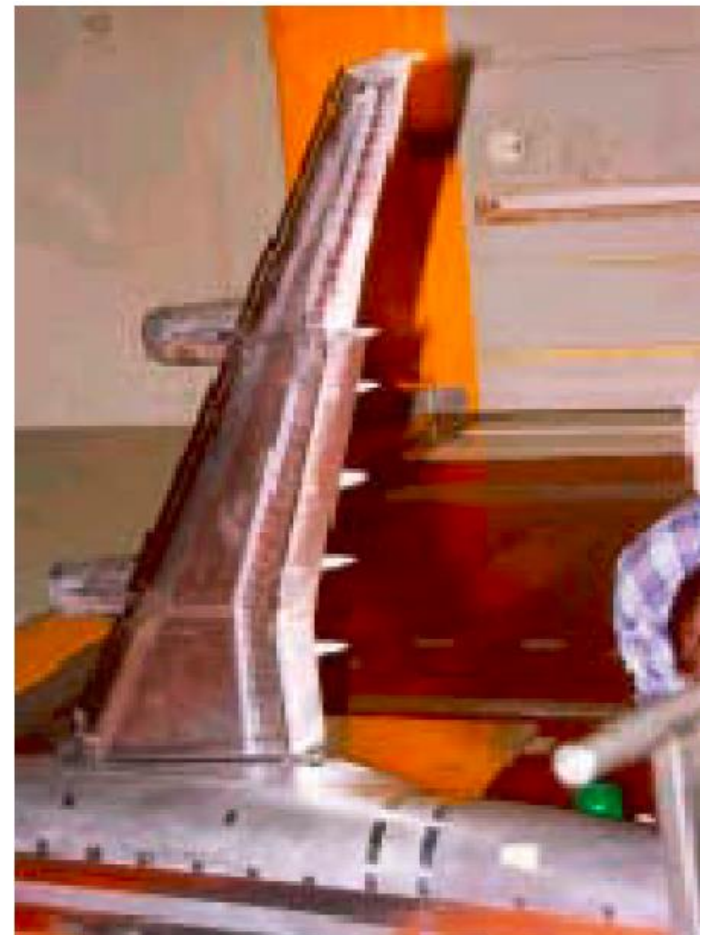
# Example – Wind-Tip vortex

- It is crucial to maintain certain distances



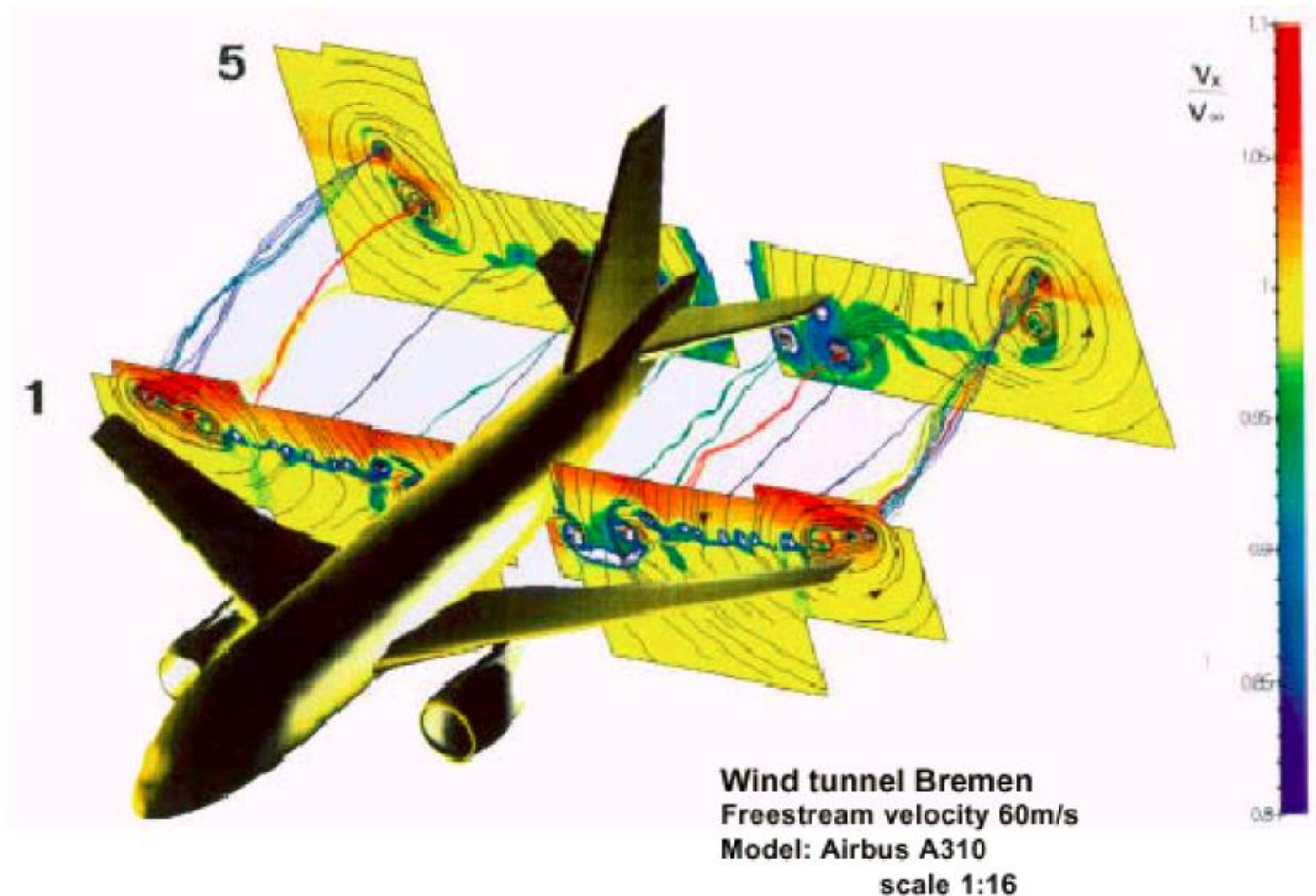
# Example – Wind-Tip vortex

- Simulation in wind tunnel



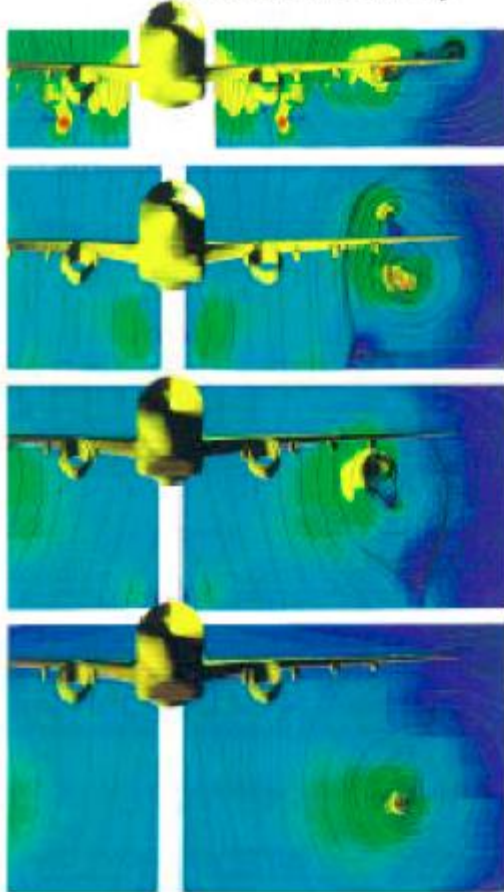
# Example – Wind-Tip vortex

- And subsequent visualization



**DNW tunnel**  
**Freestream velocity 60m/s**

Crossflow velocity



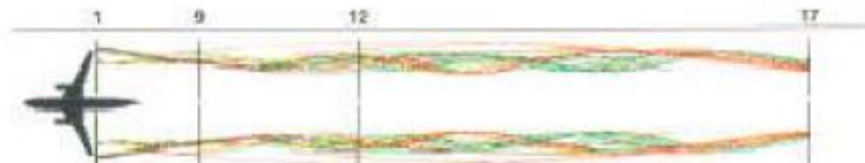
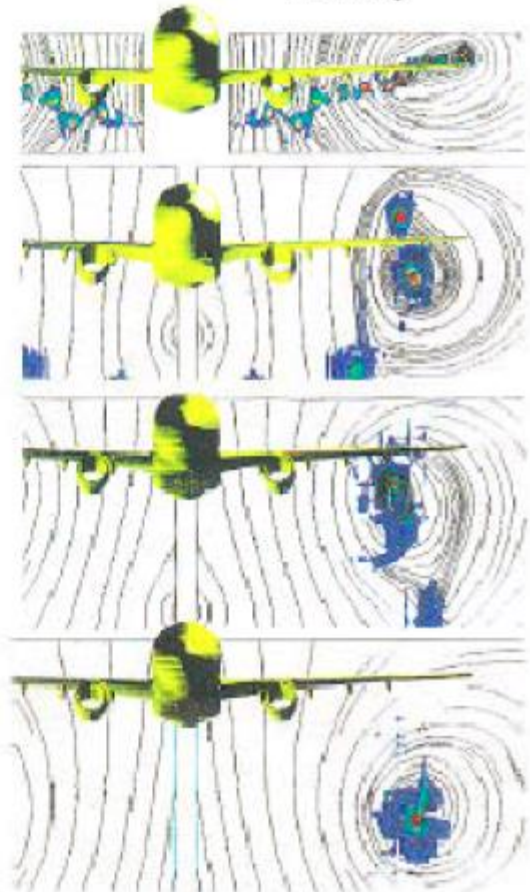
Surveying plane 1  
 0.03 wing spans behind wing tip

Surveying plane 9  
 1 wing spans behind wing

Surveying plane 12  
 2.5 wing spans behind wing

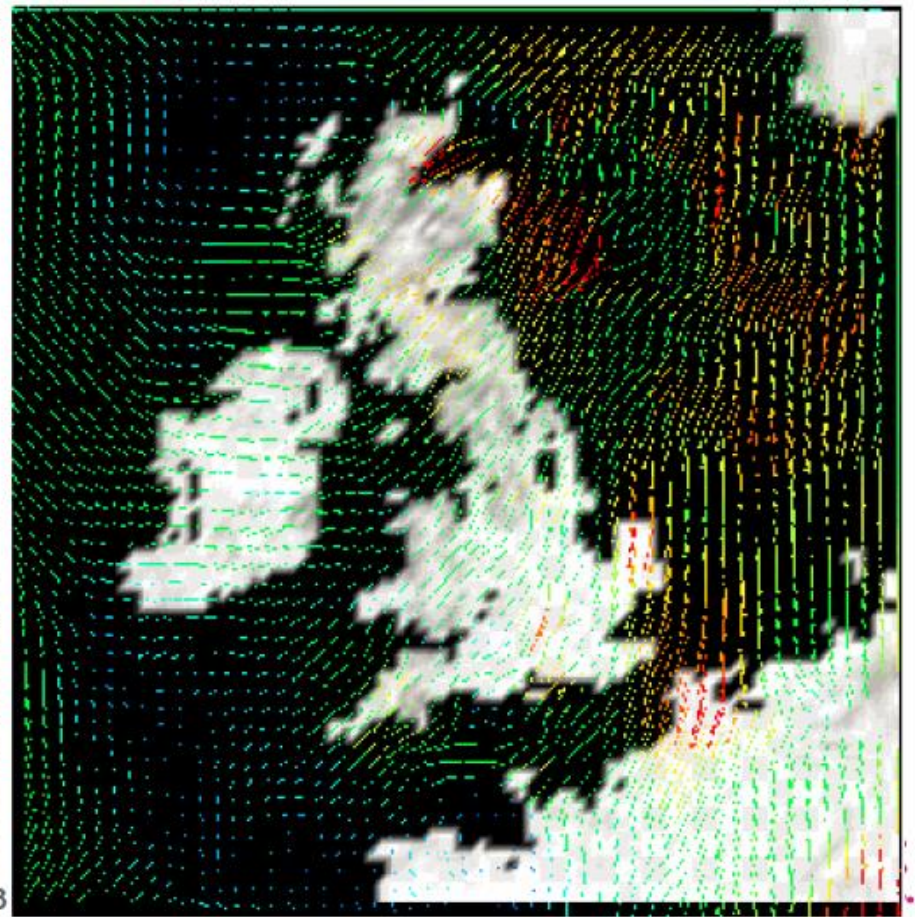
Surveying plane 17  
 6.8 wing spans behind wing

Vorticity



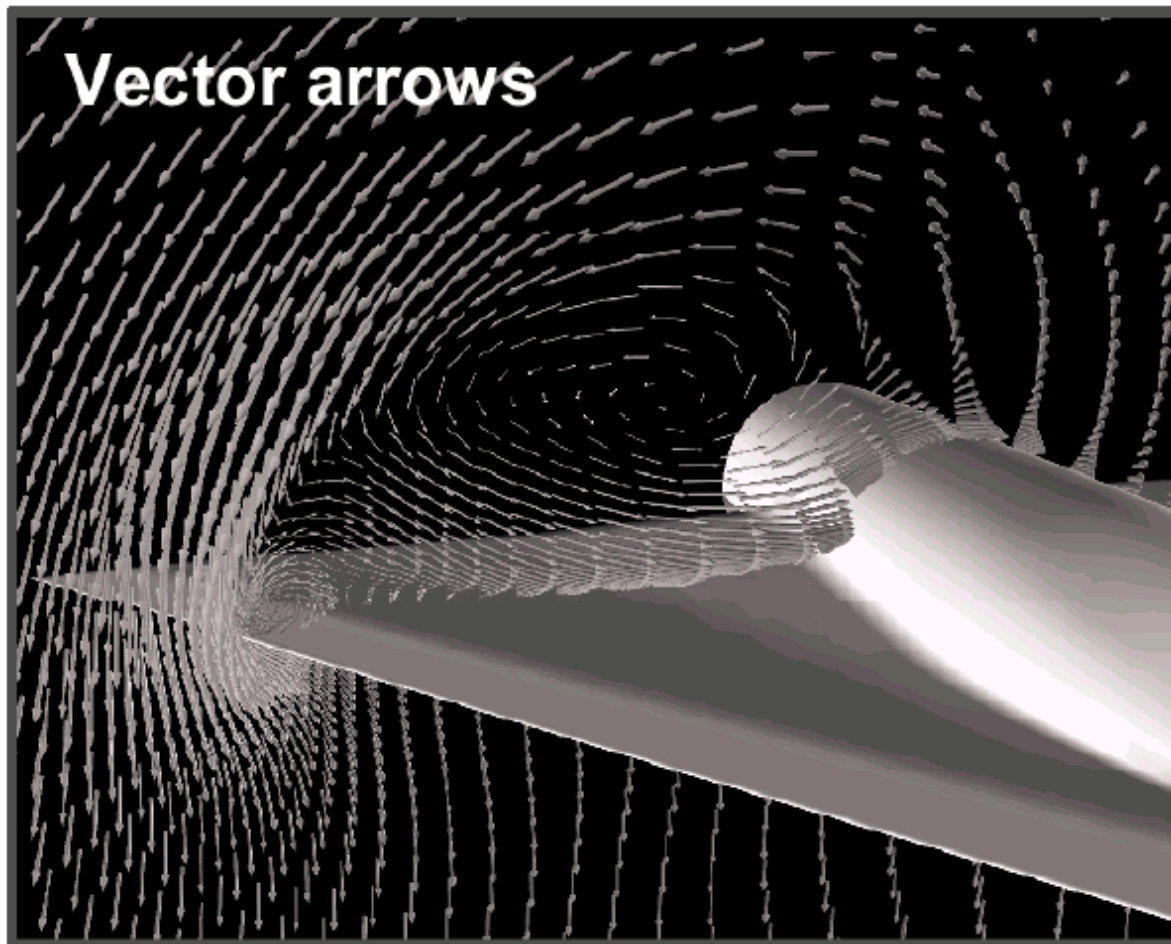
# Flow visualization using arrows

- 2D – scaling vs. coloring of arrows



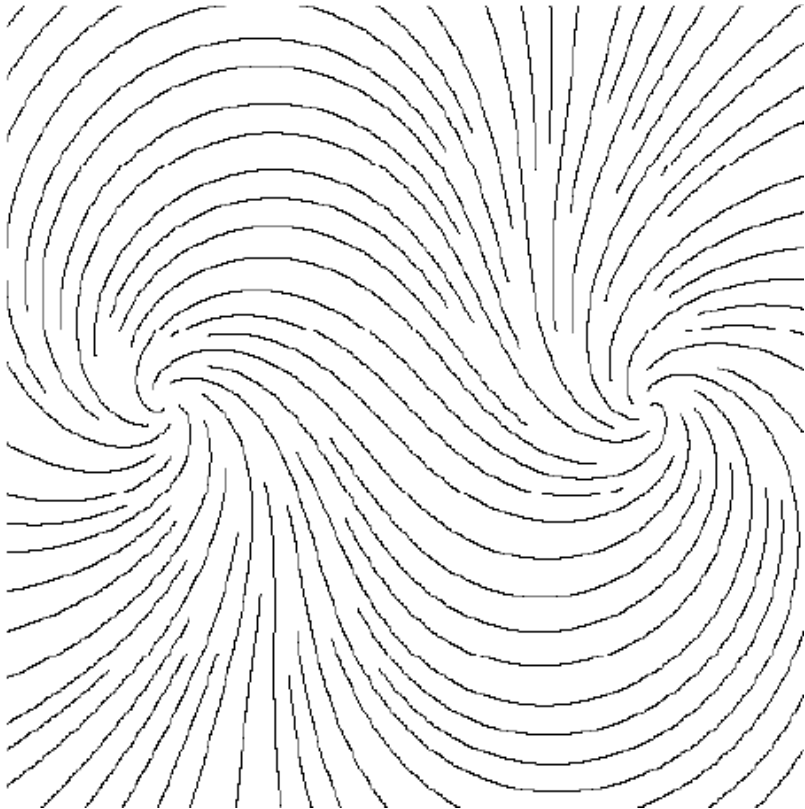
# Flow visualization using arrows

- 3D – arrows only in certain „layers“

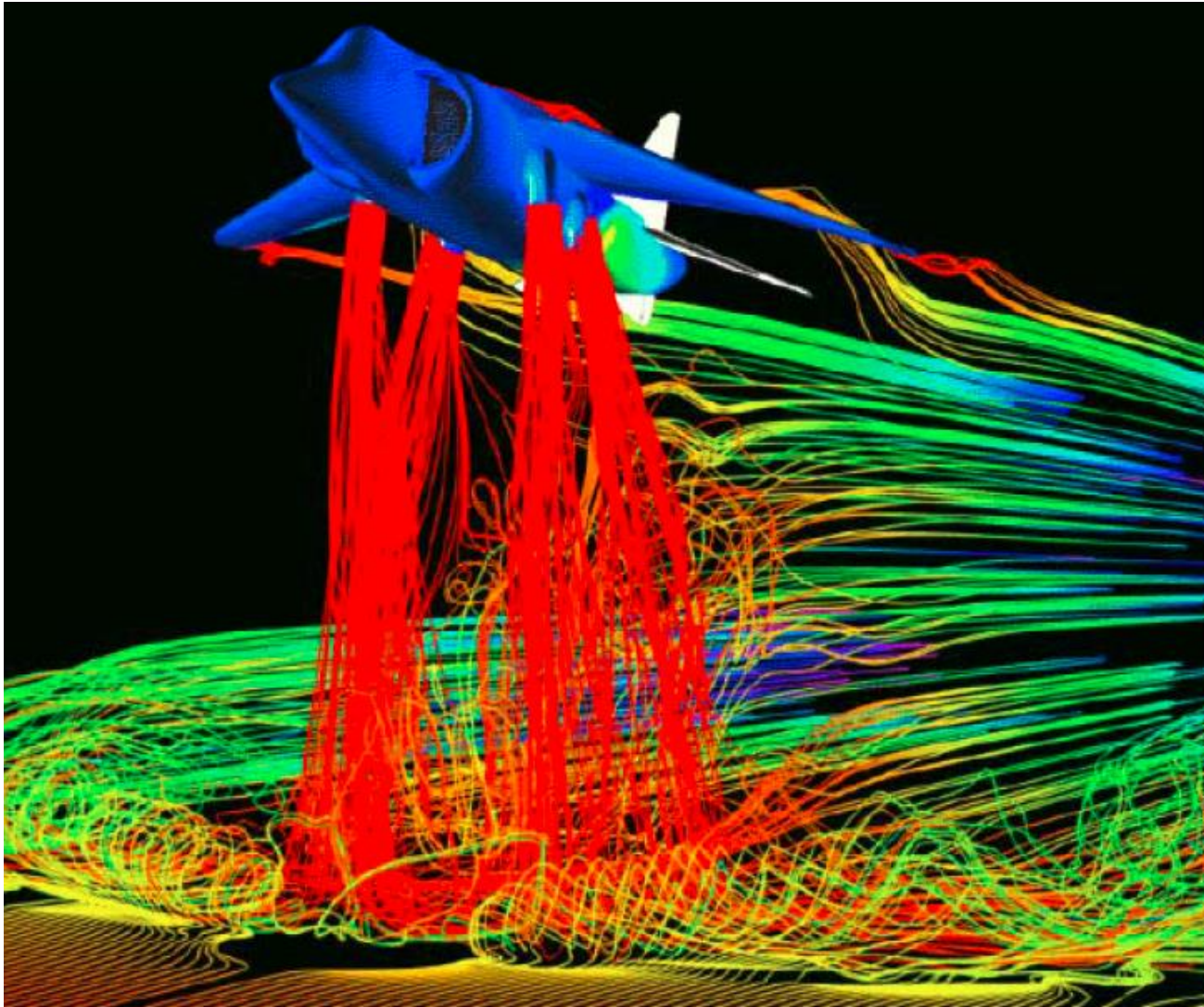


# Flow visualization using streamlines

- Streamlines = paths of individual particles in the flow



# Streamlines in 3D



# Algorithm –positioning of streamlines

- Main idea: streamlines should not be too close to each other
- Principle:
  - Parameters:
    - $d_{sep}$  starting distance
    - $d_{test}$  minimal distance

# Algorithm –positioning of streamlines

- Calculate initial streamline, insert it into queue
- Set the initial streamline as active

WHILE not finished DO

    TRY get new point in  $d_{sep}$  distance from the active streamline

    IF found THEN calculate new streamline and insert to queue

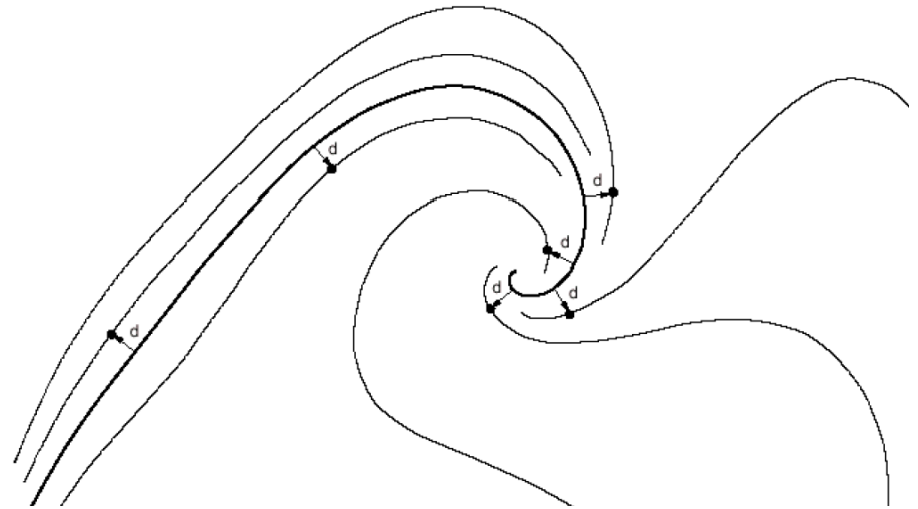
    ELSE IF queue is empty

        THEN end loop

        ELSE next streamline in queue becomes active

# Finishing generation of streamlines

- When the distance to the neighboring streamline  $\leq d_{test}$
- When the streamline leaves the predefined domain
- When the streamline is too close to itself
- After a predefined number of steps

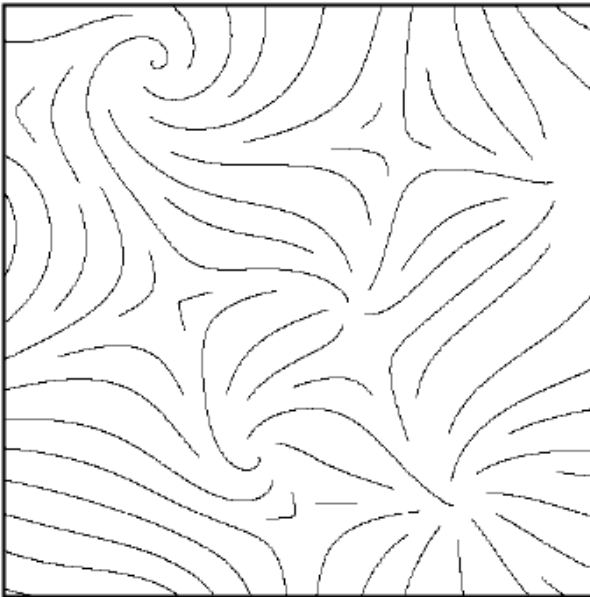


# Streamlines – influence of density by

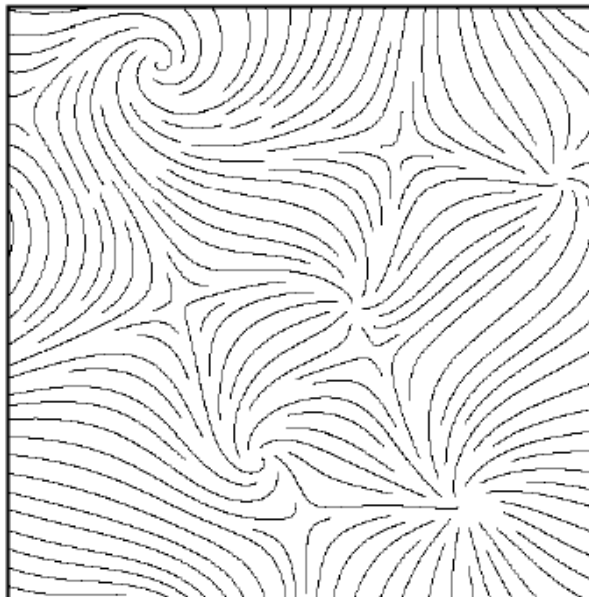
$$d_{sep}$$

- Relative to the image width:

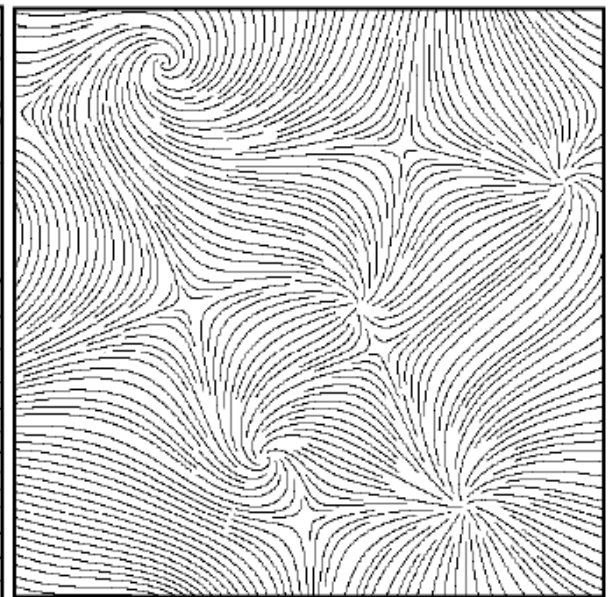
6%



3%



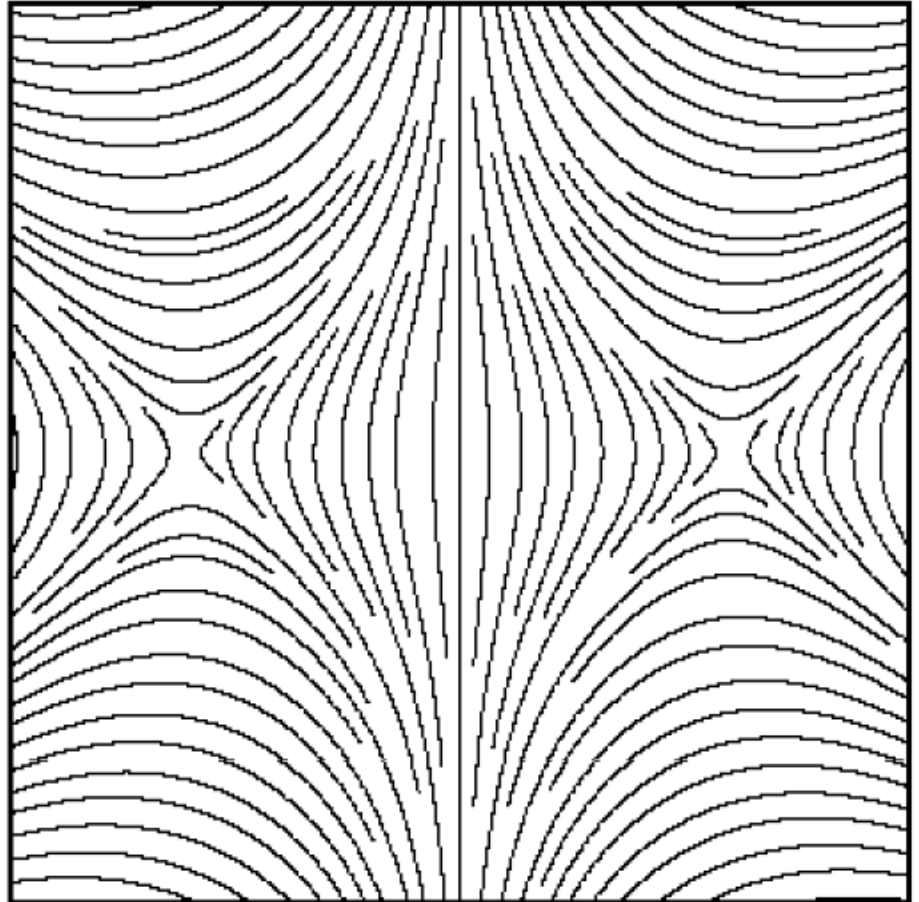
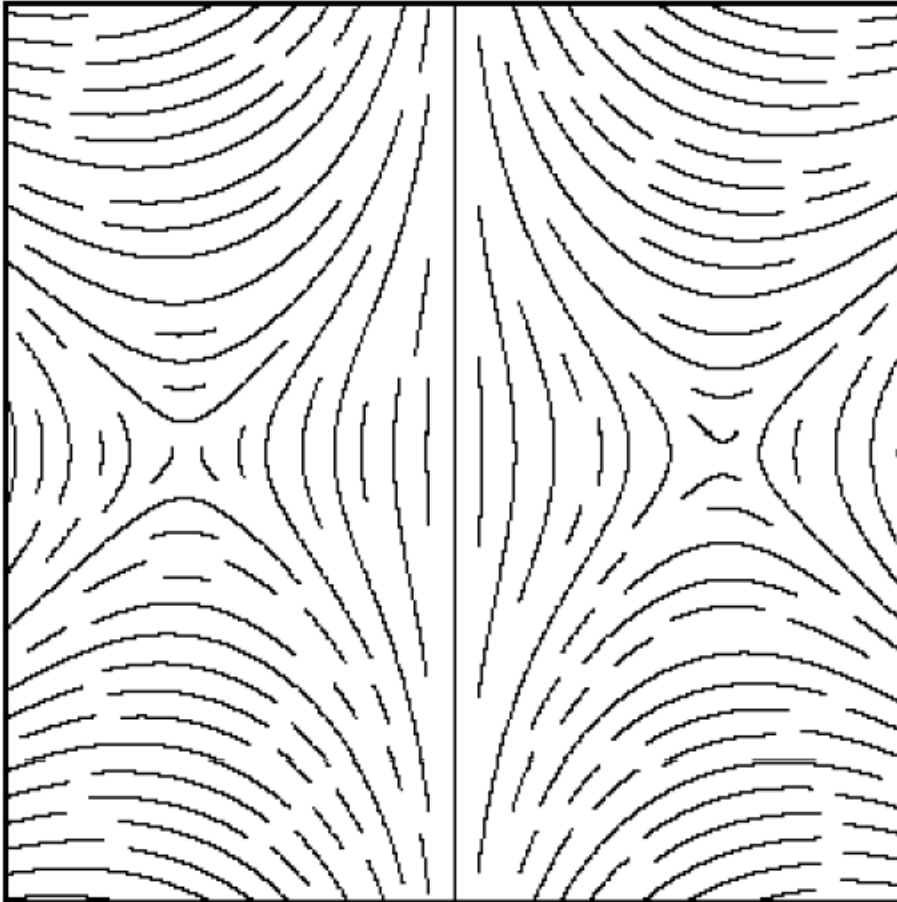
1.5%



$d_{sep}$  vs.  $d_{test}$

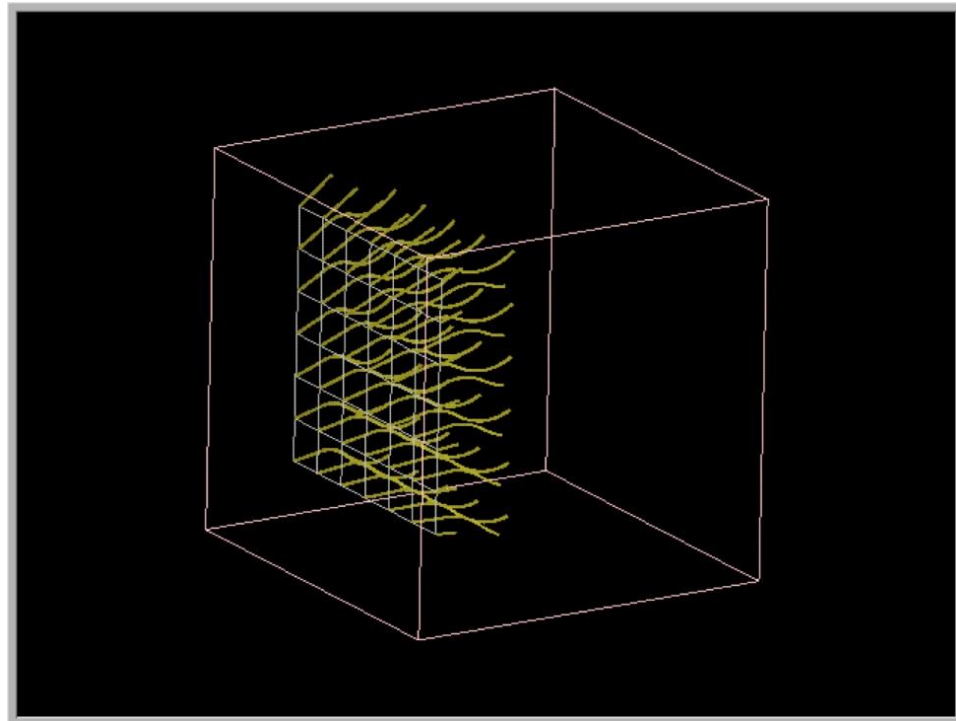
$$d_{test} = 0.9 \cdot d_{sep}$$

$$d_{test} = 0.5 \cdot d_{sep}$$

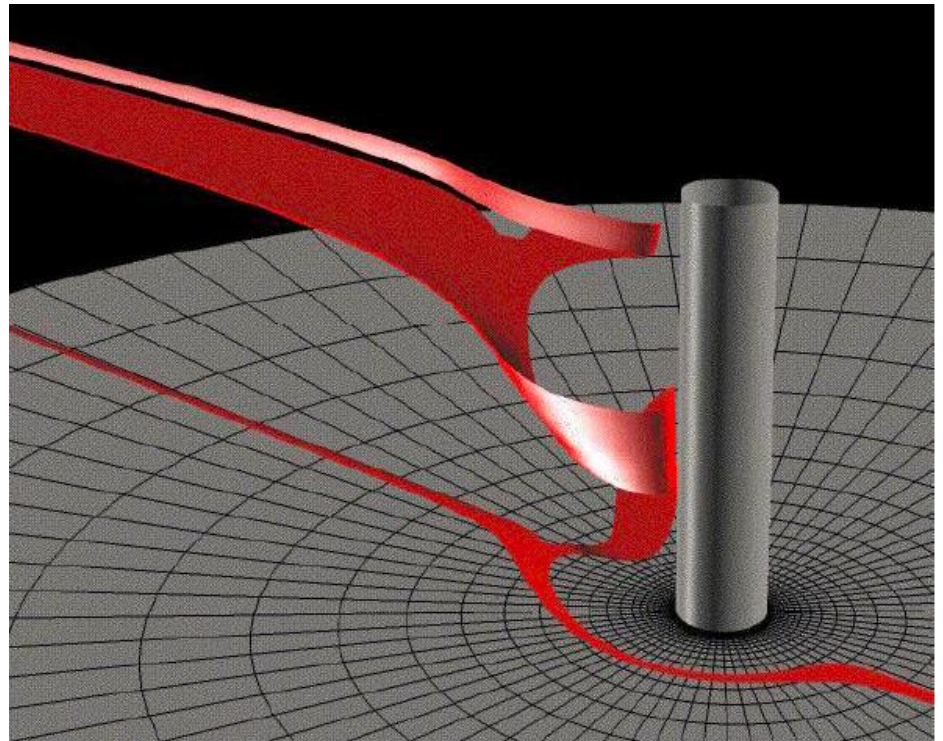
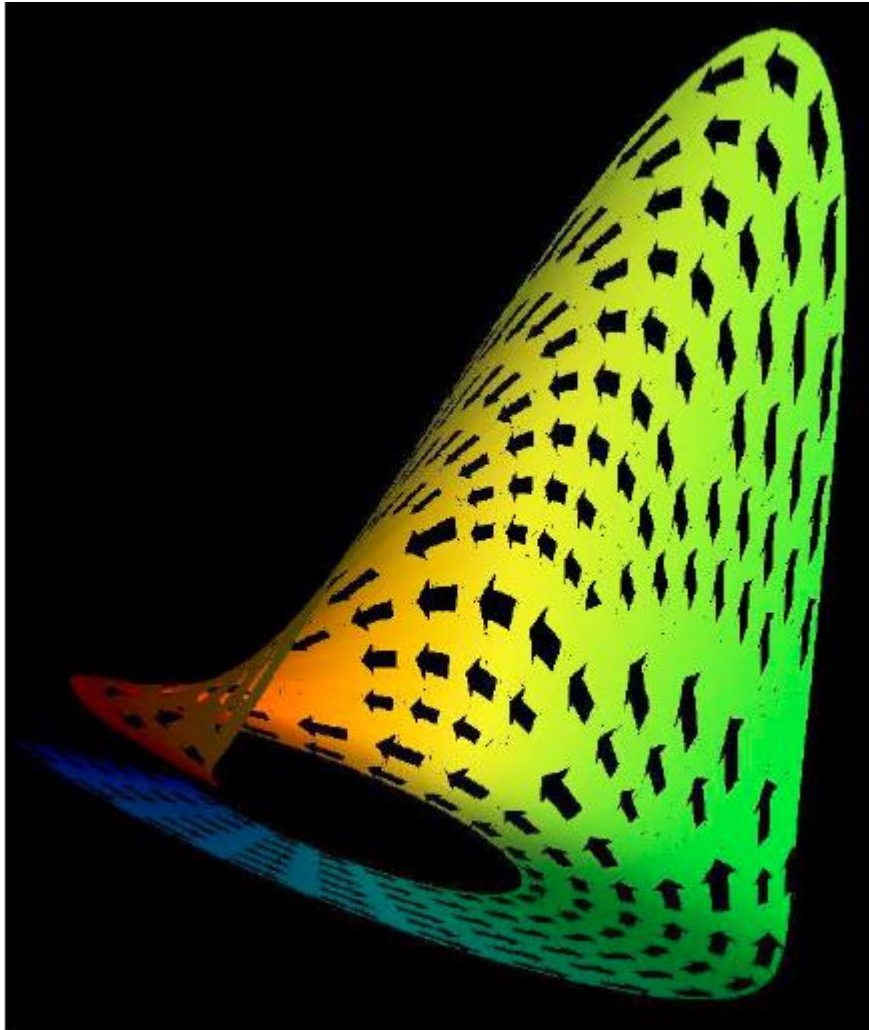


# Streaklines

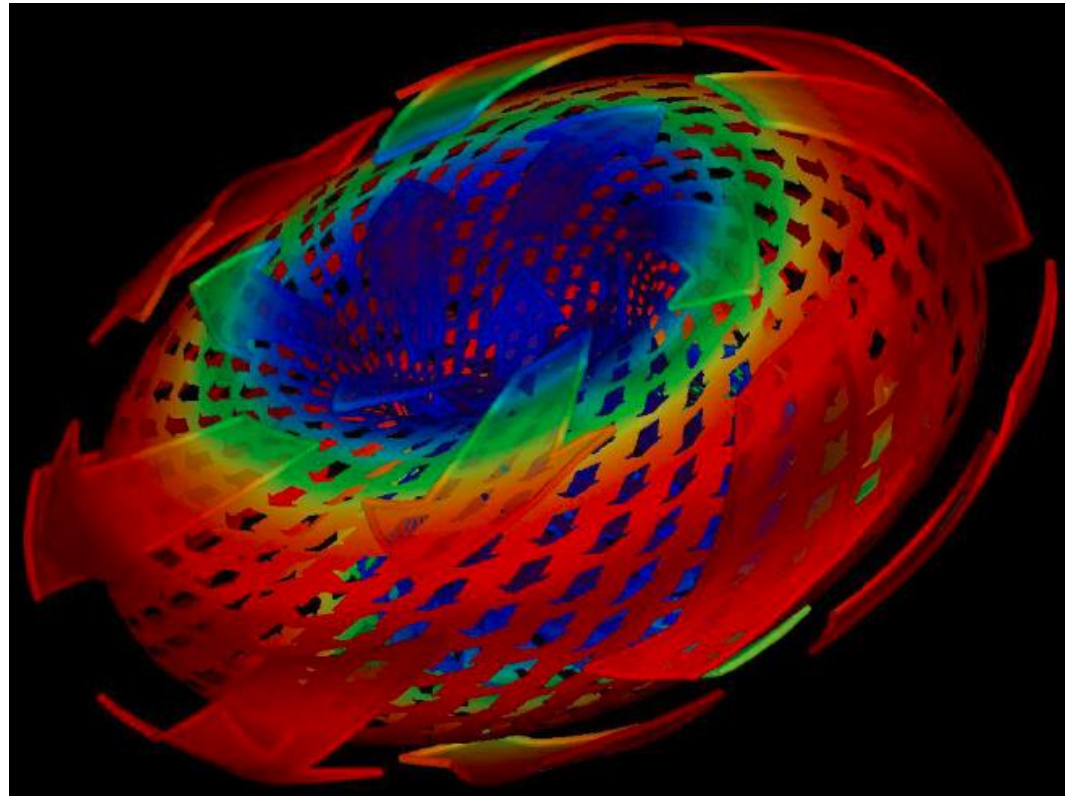
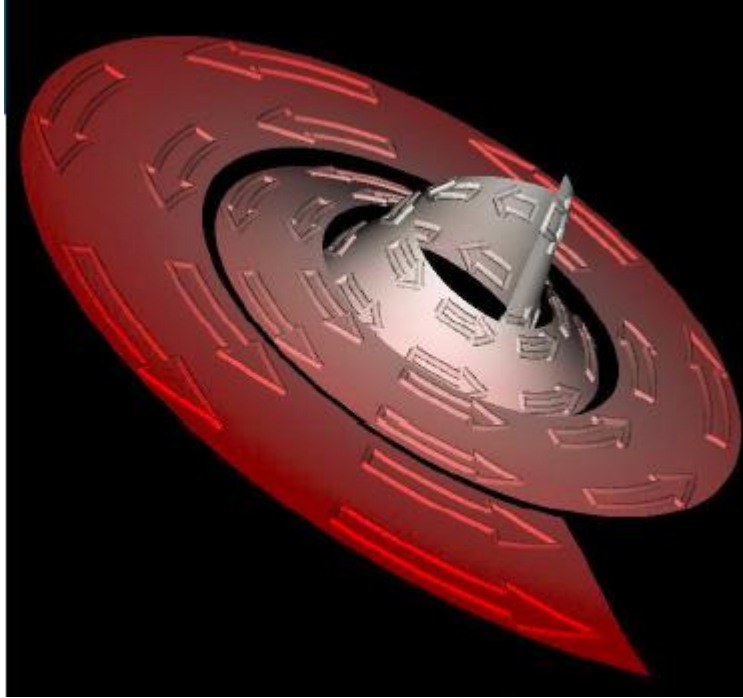
- Continuous flow of particles emitted from a discrete set of points and flowing through a field



# Streamsurfaces

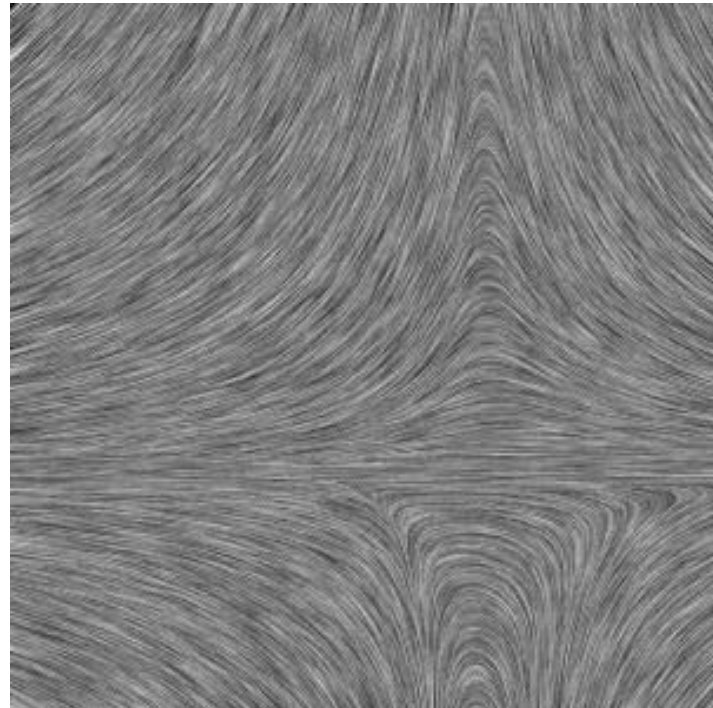


# Stream Arrows



# Line integral convolution (LIC)

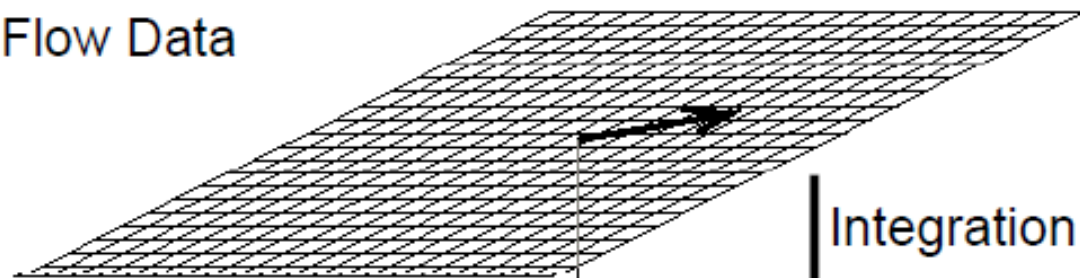
- LIC designed by Cabral a Leedom in 1993
- Random field and vector field of the same height for generating dense flow visualization



# Line integral convolution (LIC)

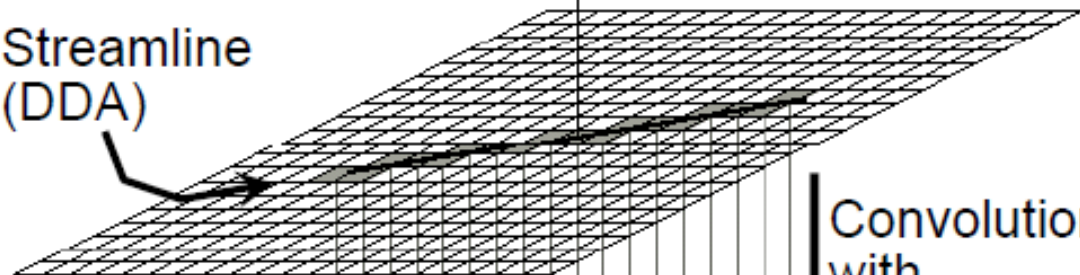
- Uses textures for showing correlation between visualization and flow
- Calculating the texture value
  - View onto streamline from a given point
  - Filtration of white noise along streamline

Flow Data



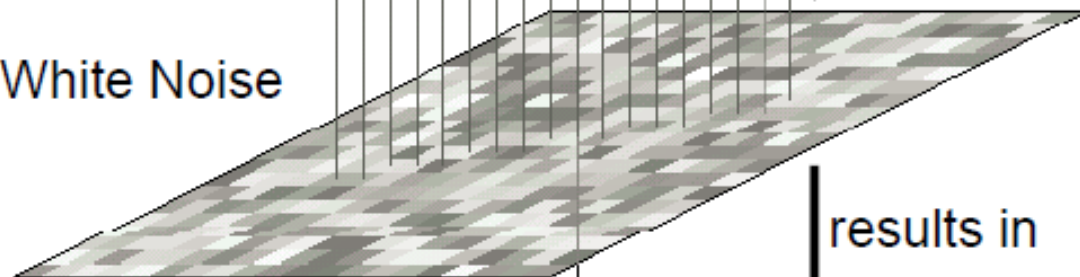
Integration

Streamline  
(DDA)



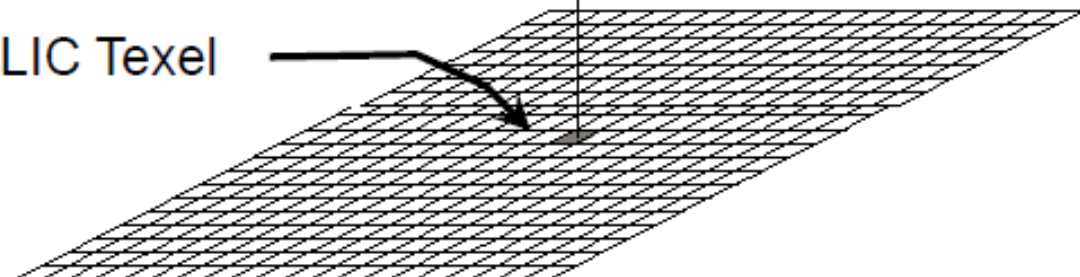
Convolution  
with

White Noise

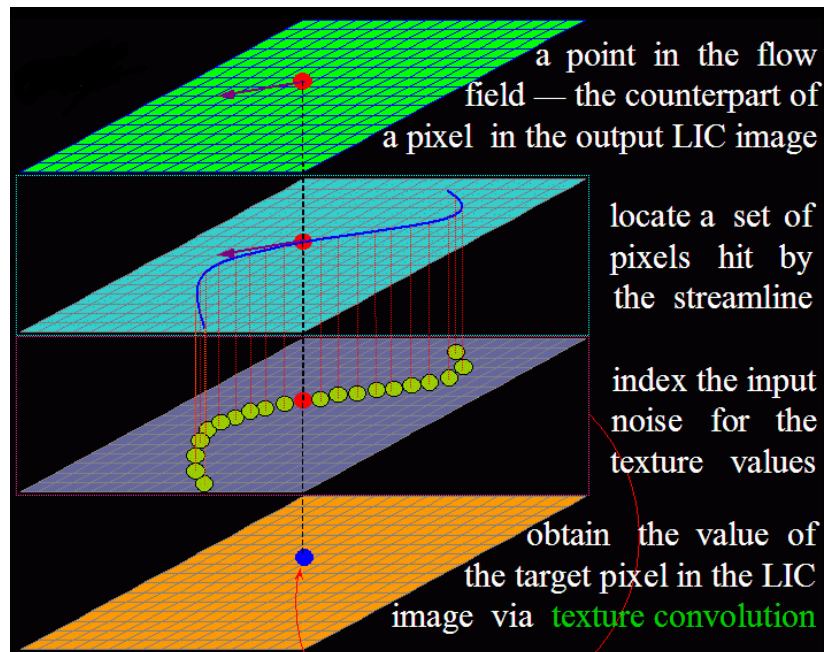
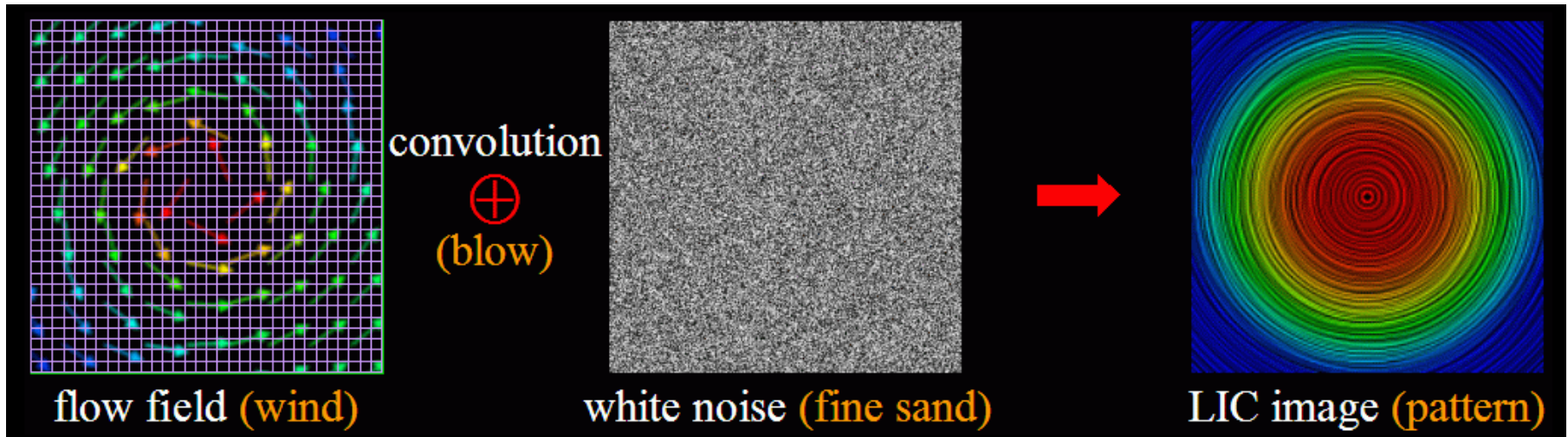


results in

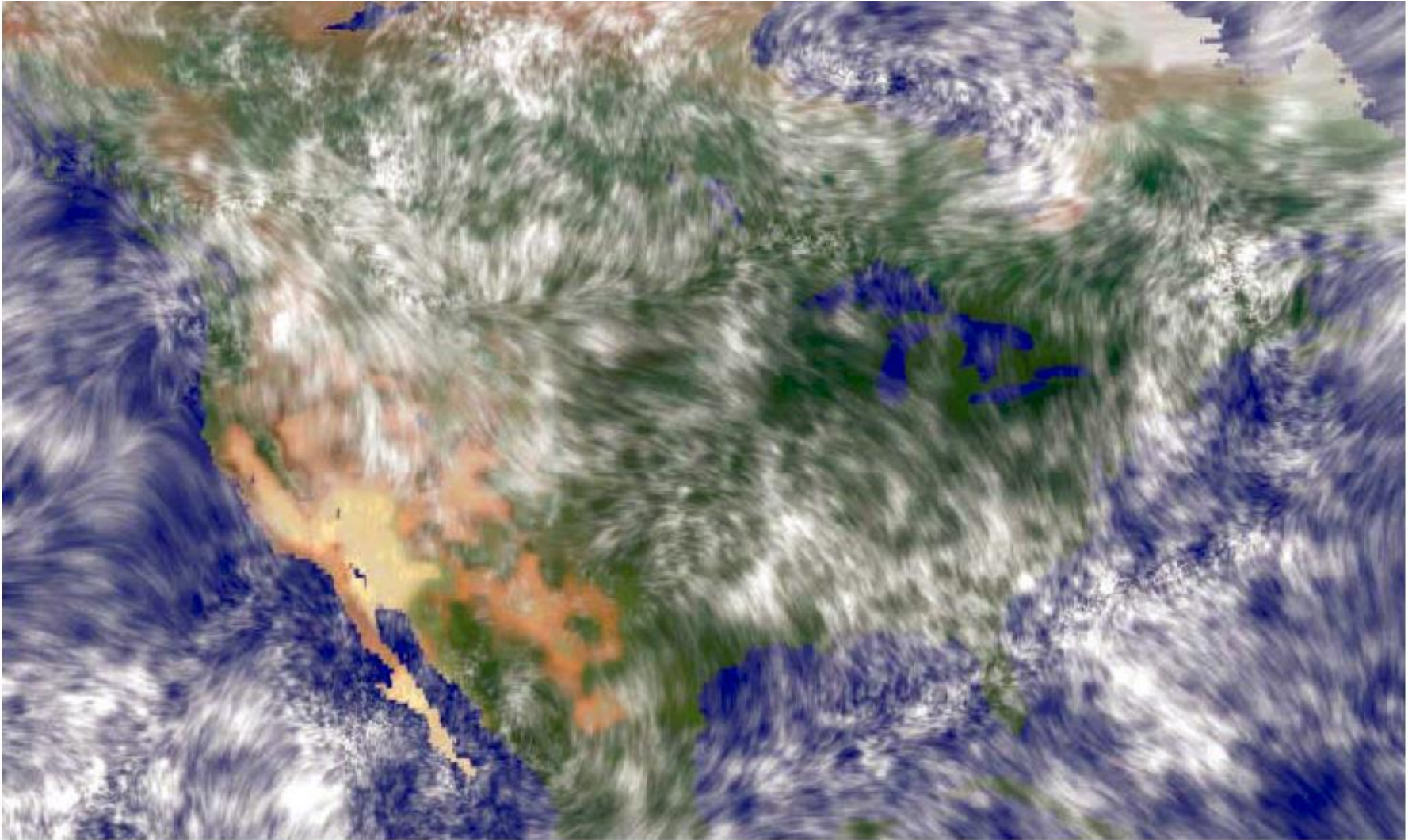
LIC Texel



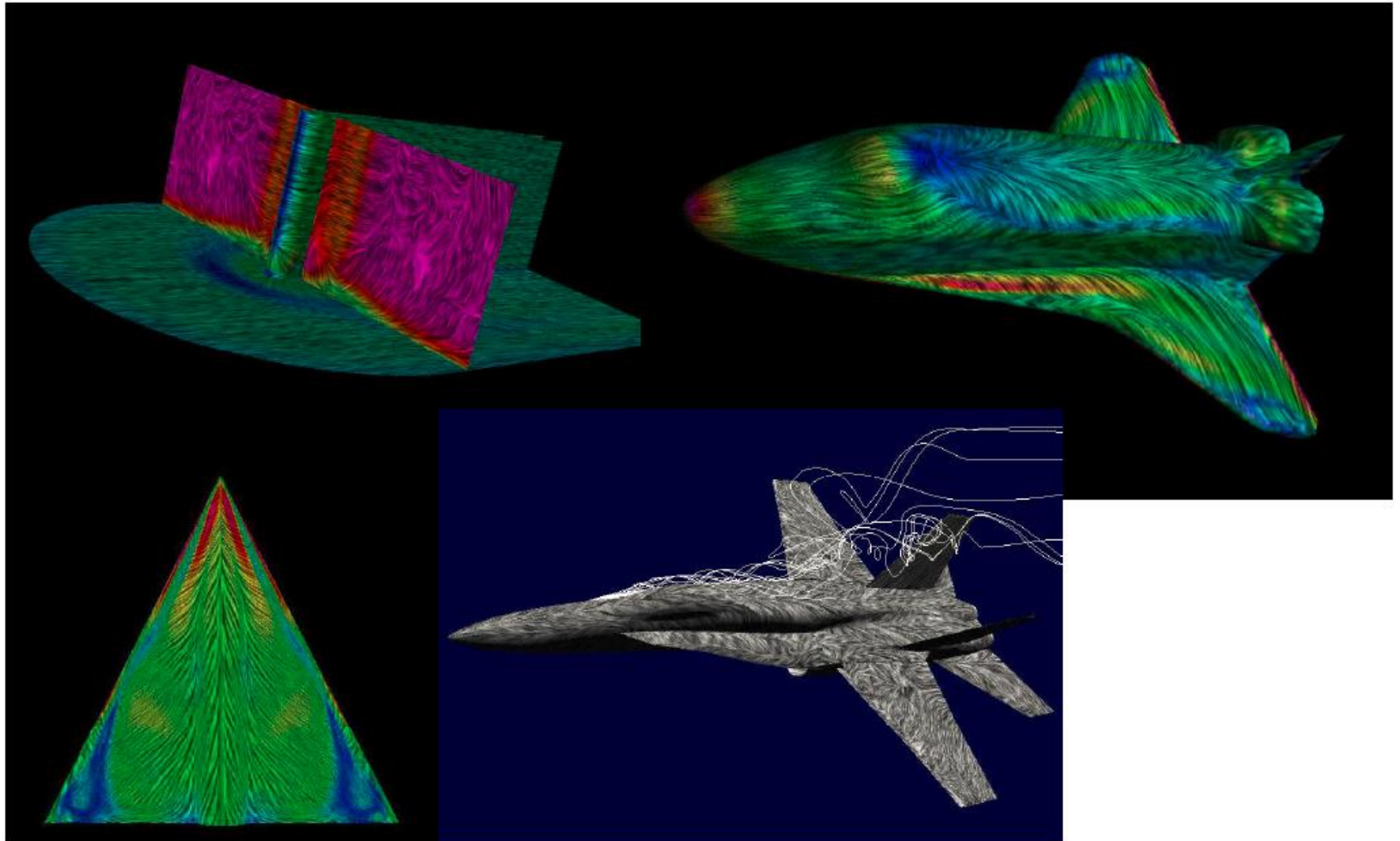
# LIC



# LIC examples

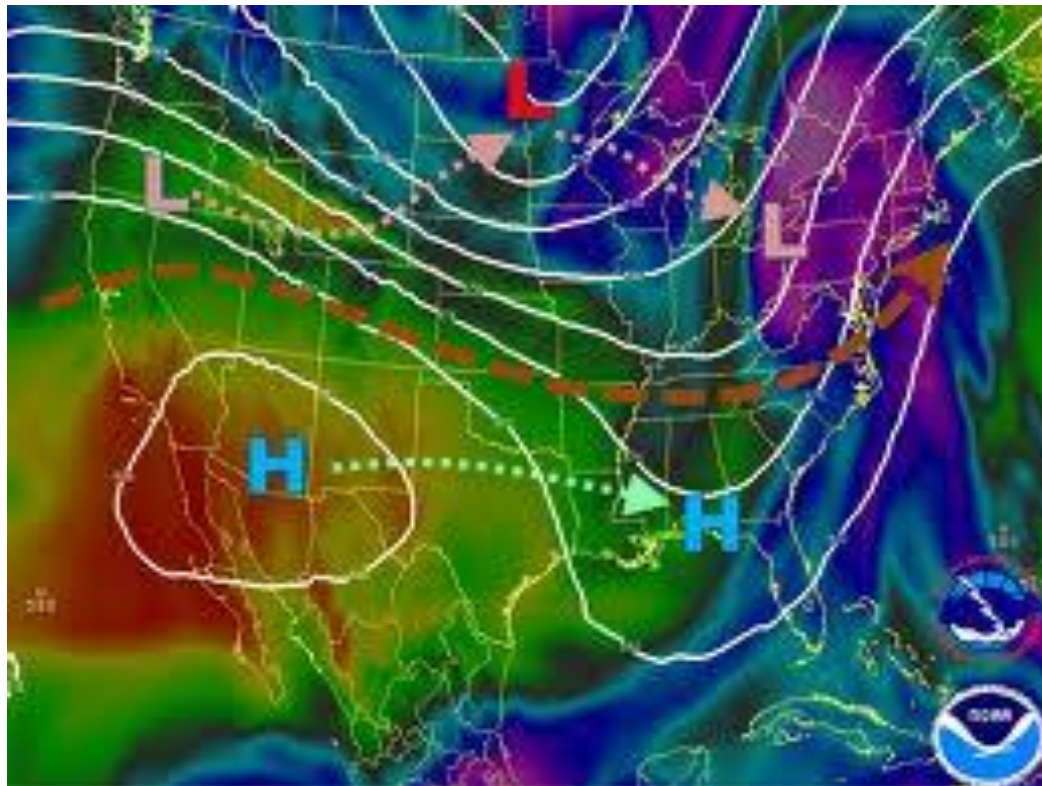


# LIC – mapping onto surface



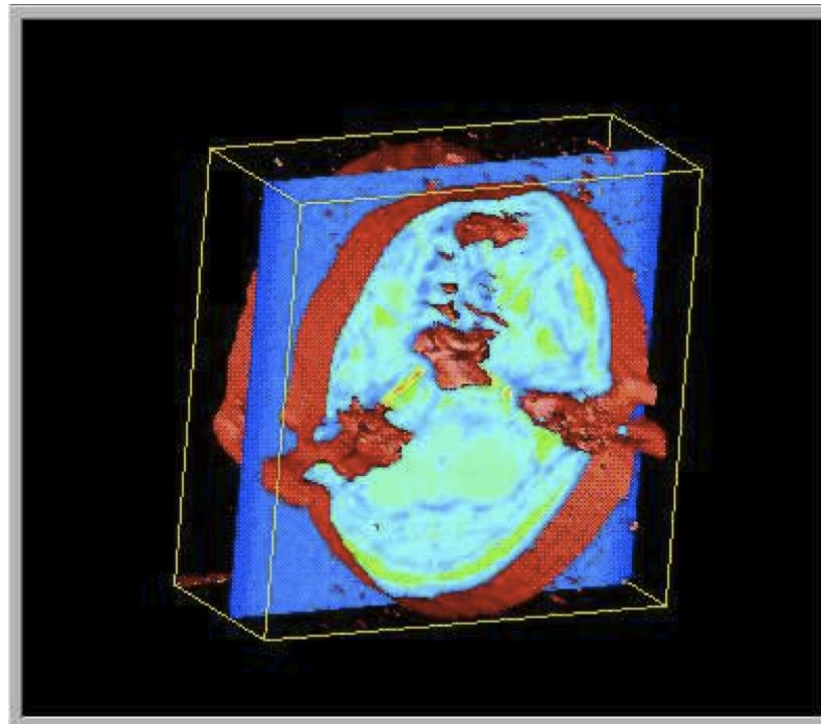
# Combined techniques

- Combination of techniques enables to highlight their strong points



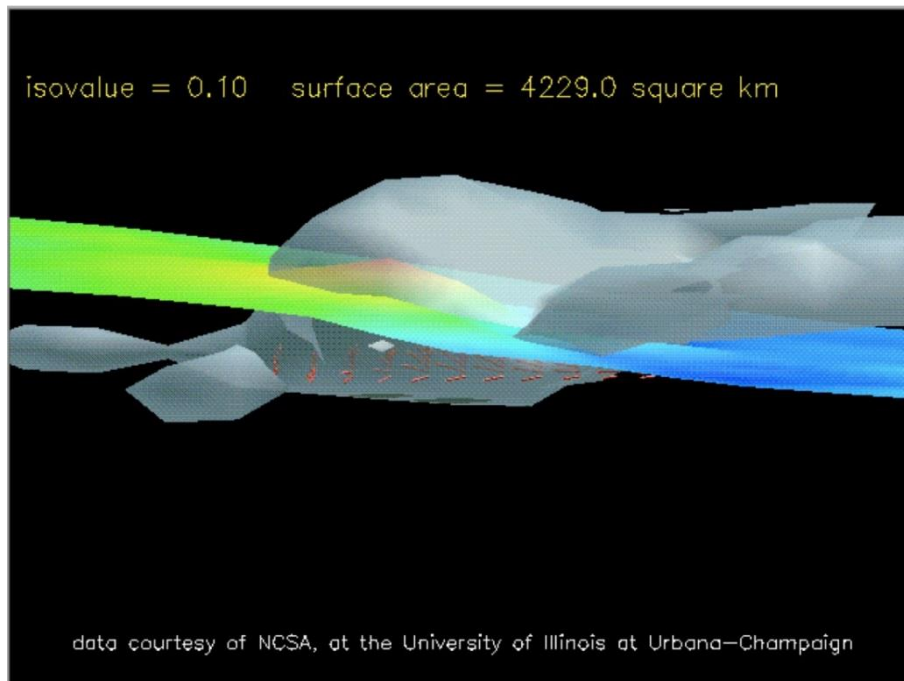
# Slices combined with isosurfaces

- Isosurface of medical data in combination with orthogonal slicing
- [Video](#)

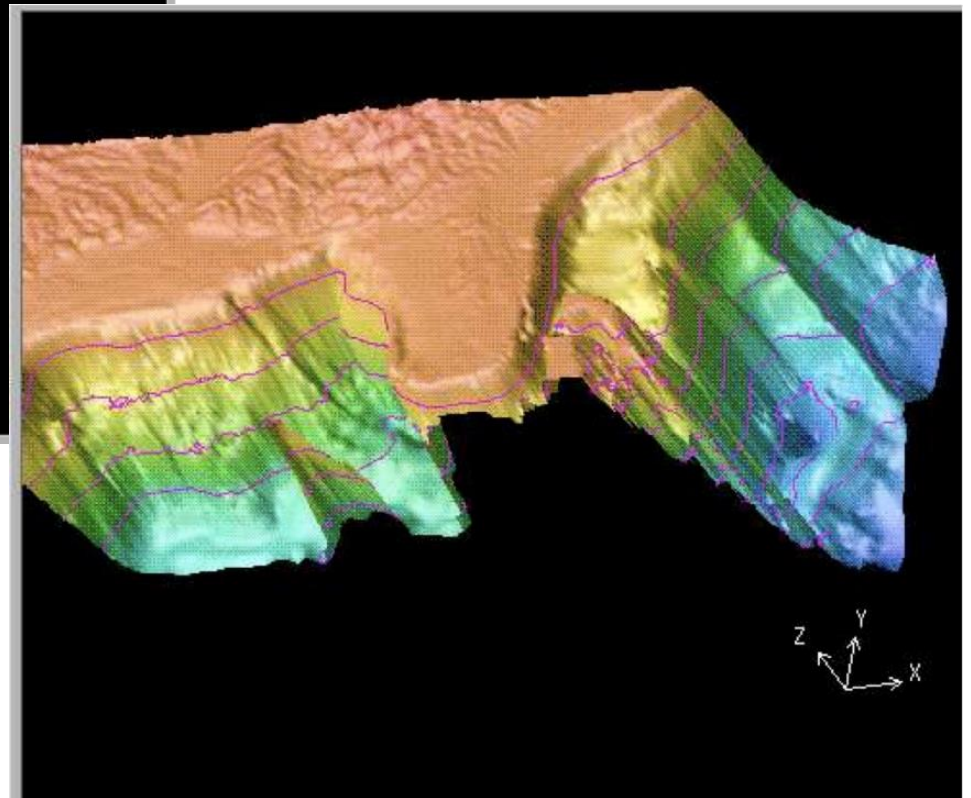
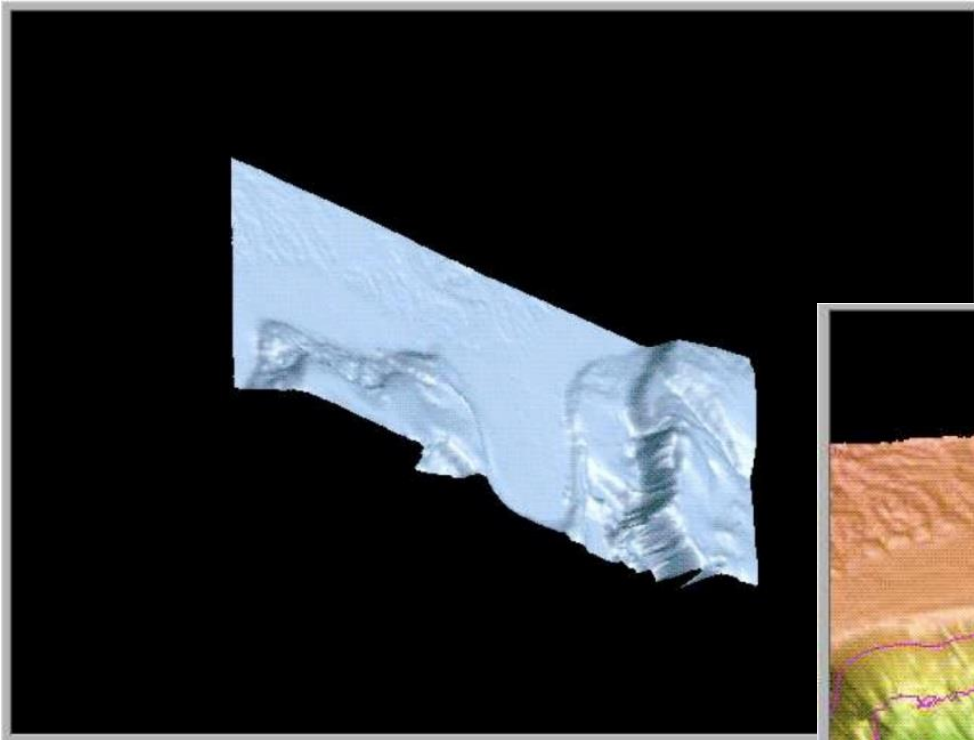


# Combining isosurfaces and pictograms

- Isosurfaces for showing details of 3D surface, pictograms for showing size or direction of change in the dataset

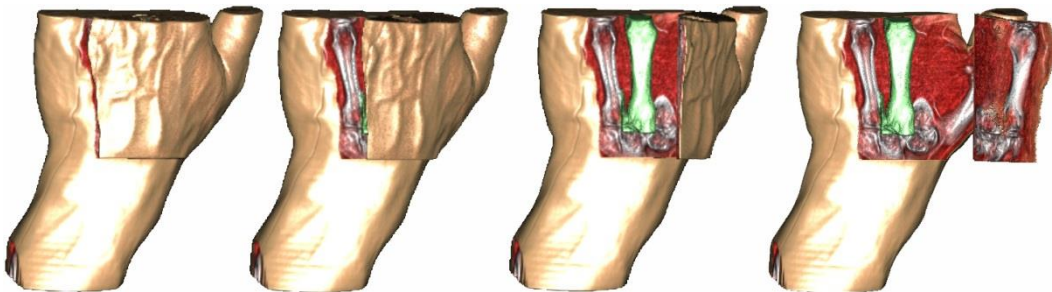


# Surface + contour + color

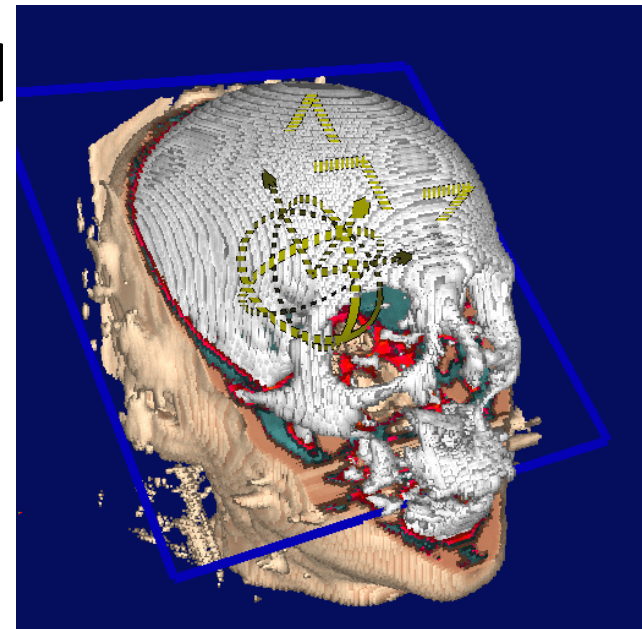


# Summary

- Different techniques for data in different dimensions
- We need to understand pros and cons of the techniques
- Their combination is beneficial



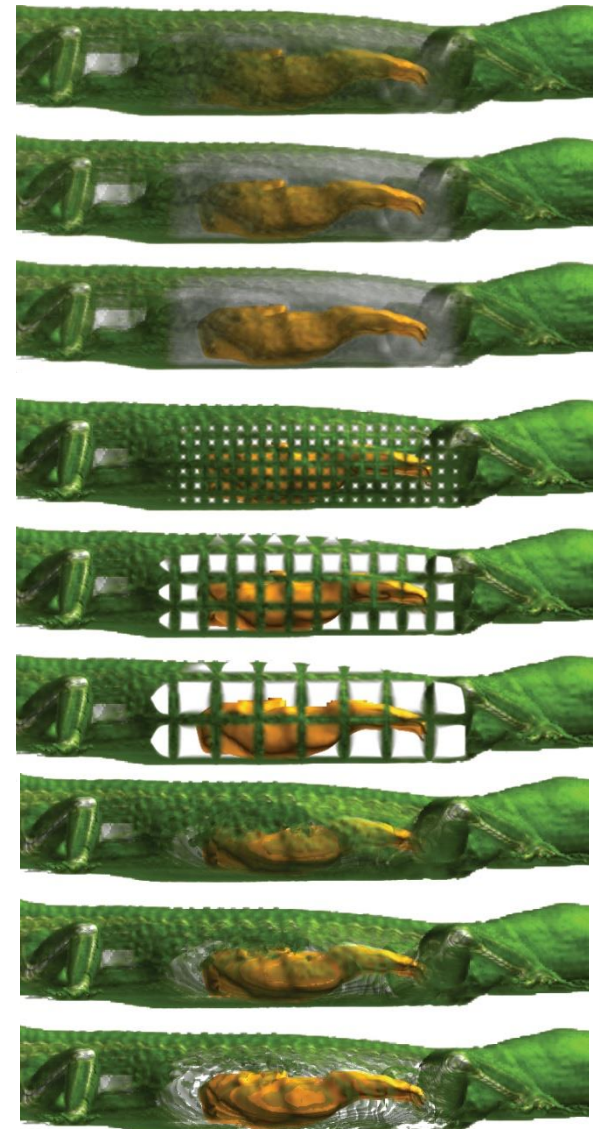
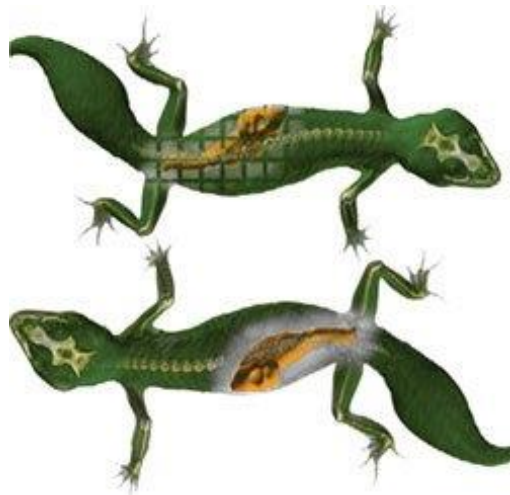
[www.ii.uib.no](http://www.ii.uib.no)



[profs.etsmtl.ca](http://profs.etsmtl.ca)

# Examples

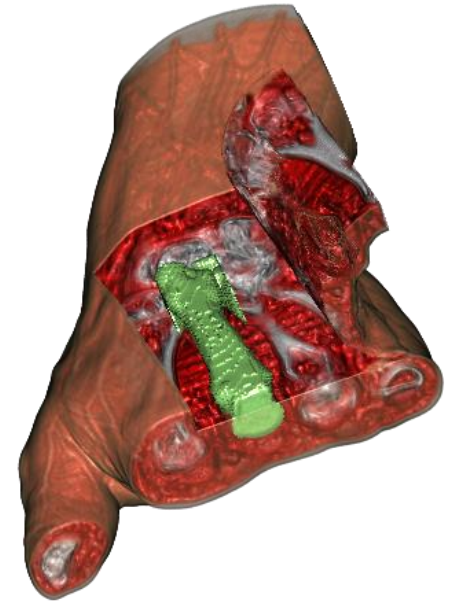
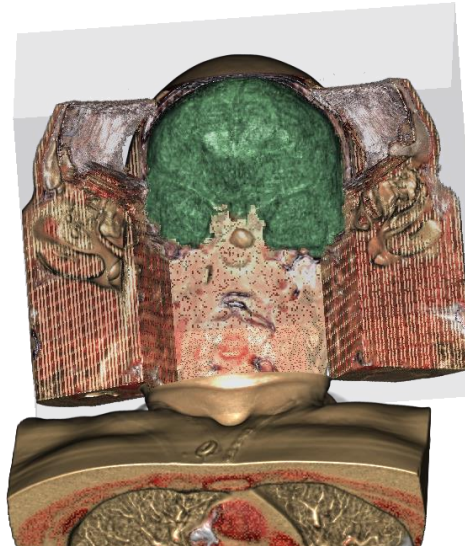
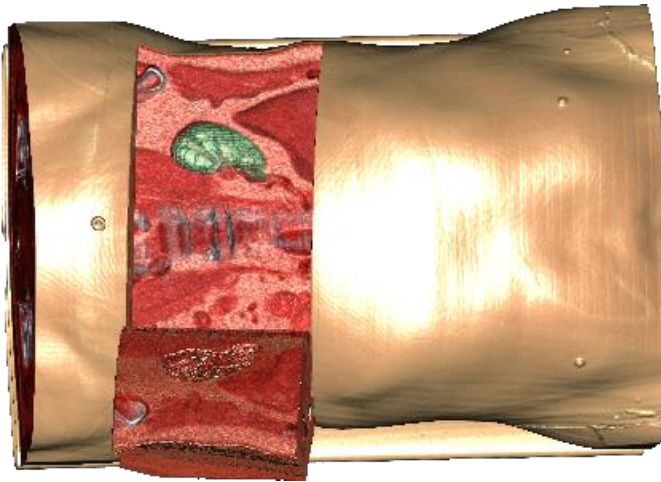
- Ivan Viola – Importance-Driven Volume Rendering



- <http://www.cg.tuwien.ac.at/research/publications/2004/Viola-2004-ImpX2/>

# Examples

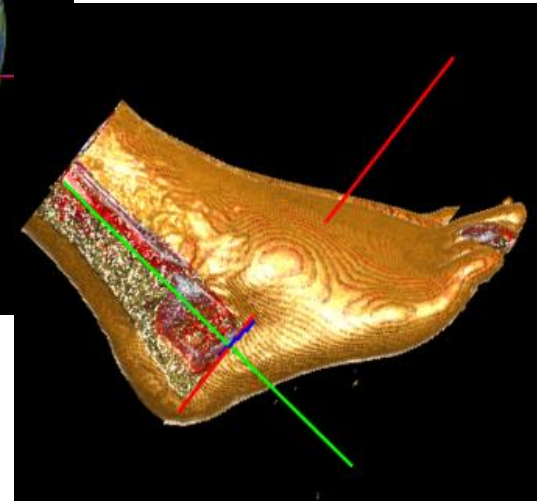
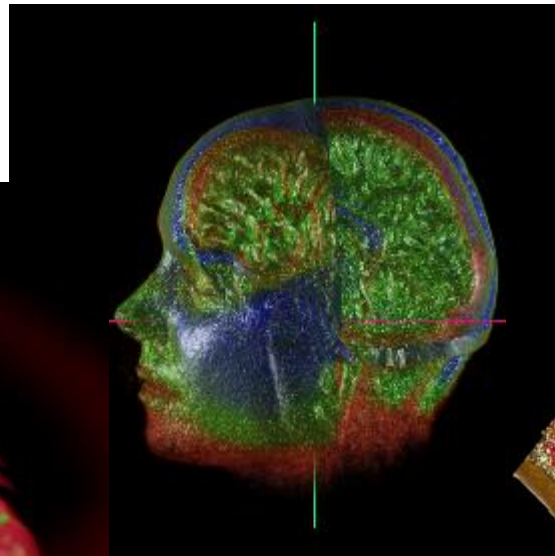
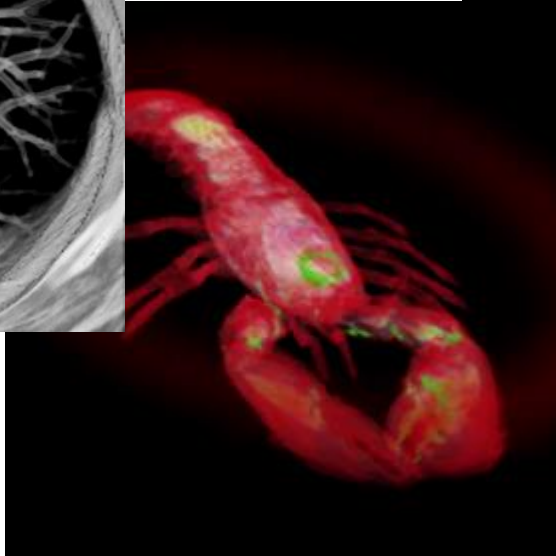
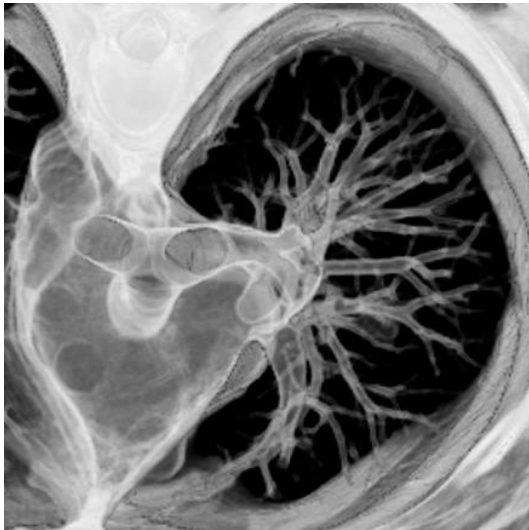
- Åsmund Birkeland - View-Dependent Peel-Away Visualization for Volumetric Data



- <http://www.ii.uib.no/vis/teaching/thesis/2008-birkeland/files/MasterThesisBirkeland2008.pdf>

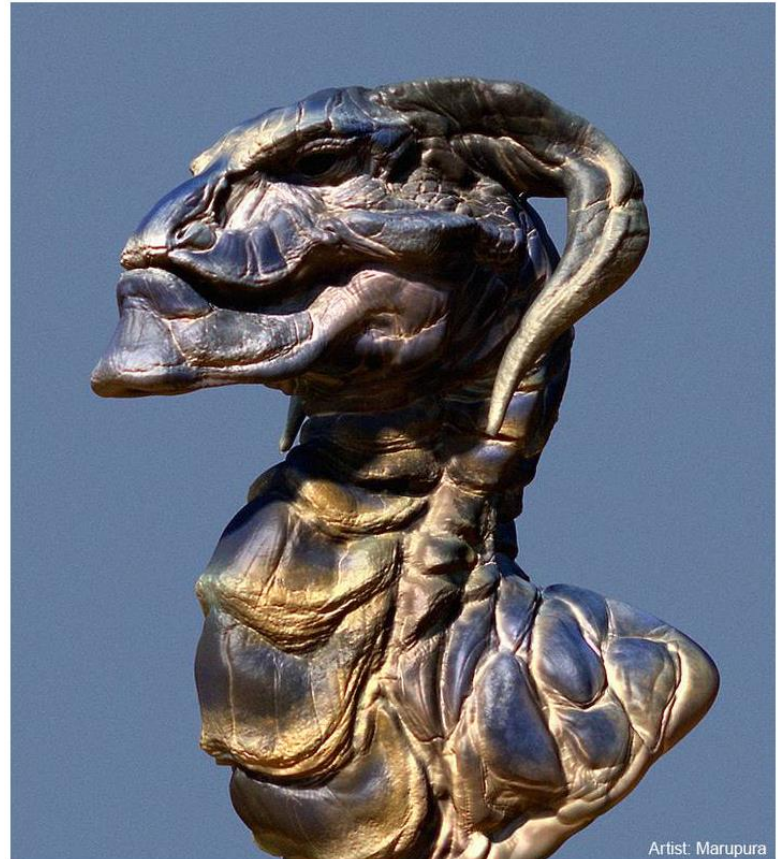
# Examples

- Meißner et al., Volume Visualization and Volume Rendering Techniques, EUROGRAPHICS 2000



# Voxel modeling

- 3D-Coat modeling tool
  - Voxel-based modeling



<http://3d-coat.com/voxel-sculpting/>