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6. Trees, Graphs, Networks

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Relationships Between Data

- Hierarchical relationships
- Interconection, continuity
- Derivation (sequence)
- Shared classification
- Similarity of values
- Similarity of attributes



Visualization of Hierarchical Structures

- Hierarchical structures = trees
- Algorithms for visualization:
 - Space-filling maximal usage of screen space

Non-space-filling



Space-filling Methods

- Two most common types:
 - Rectangular layout
 - Treemaps
 - Radial layout
 - Sunburst view





Treemap - Pseudocode

Naming:

Width = width of the rectangle Height = height of the rectangle Node = root node of the tree Position = position of rectangle (e.g., [0, 0]) Orientation = orientation of the split - alternating horizontal and vertical split

treemap(Node n, Orientation o, Position orig, Width
w, Height h)

treemap(Node n, Orientation o, Position orig, Width w, Height h)

if n is the leaf node (has no child nodes)
 draw_rectangle(orig, w, h);

return;

for each child node of the n (child i)

get number of leaf nodes in the subtree; sum up the total number of the leaf nodes; compute the percentage of leaf nodes in each subtree (percent_i);

if orientation is horizontal

for each subtree

compute the offset of the origin based on the origin and the width (offset_i); treemap(child_i, vertical, orig+offset_i, w*percent_i, h);

else

for each subtree

```
compute the offset of the origin based on the
origin and the height (offset_i);
treemap(child_i, horizontal, orig+offset_i, w,
h*percent_i);
```





Radial Layout

- Sunburst displays
- Root of the hierarchy placed in the center of the radial view, individual layers of hierarchy represented by concentric rings
- Rings are split based on the number of nodes at the given level
- Radial techniques display inner nodes as well as leaves

Sunburst - Pseudocode

Naming:

Start = start angle of the node (initially 0)
End = end angle of the node (initially 360)
Origin = position of the center of the radial view
 (e.g., 0, 0])
Level = current level of hierarchy (initially 0)
Width = width of each ring - based on maximal depth
 of the hierarchy and the size of display

sunburst(Node n, Start st, End en, Level 1)

sunburst(Node n, Start st, End en, Level 1)

if n is the leaf node (has no child nodes)
 draw_radial_arc(Origin, st, en, l*Width,
 (l+1)*Width);

return;

for each child nod of the n (child i)

get number of leaf nodes in the subtree; sum up the total number of the leaf nodes; compute the percentage of leaf nodes in each subtree (percent_i);

for each subtree

compute the initial/end angle based on the size of subtrees, their order and the range of angles;

sunburst(child_i, st_i, en_i, l+1);



Color in Hierarchical Techniques

- Highlighting of many attributes, e.g.:
 - Values in nodes
 - Enhancement of hierarchical relationships (similar color for parent and child nodes)

 Additional properties displayed by symbols, marks and labels placed into rectangular or radial segments

Non-Space-Filling Methods

- Node-link diagrams are the most common
- Diagrams dependent mostly on two factors:
 - Degree of the nodes (number of branches, e.g., binary trees)



Design of the Algorithms for Rendering Node-Link Graphs

- Three categories of rules:
 - Rendering conventions shape and curvature of edges, placement of the nodes into fixed grid, neighbors at the same vertical position, ...
 - Restrictions placement of the nodes at given position, displaying nodes in close proximity, orientation of edges, ...
 - Aesthetics minimization of edge intersections, keeping the width/height ratio of the graph, minimization of the overall graph area, minimization of the edge length, minimization of the edge bending, minimization of the number of different angles and curves, effort to keep the symmetry

Design of the Algorithms for Rendering Trees

- Divide the rendering area into slices of the same height – the number of slices is derived from the depth of the tree
- 2. For each level of the tree, determine how many nodes need to be drawn
- Divide each slice into rectangles of same size derived from the number of nodes at the given level
- 4. Draw each node into the corresponding rectangle
- 5. Draw connecting line leading from the center of the bottom edge of each node to the center of the top edge of the its child nodes



Optimalisation

- Improve the usage of the screen space
- Examples:
 - Each level divided by the number of leaf nodes in the corresponding subtree
 - Uniform layout of the leaf nodes + centering of their parent nodes
 - Adding additional gaps between neighboring nodes that do not have common parent (i.e., are not siblings)
 - Reorganization of the tree in order to improve the symmetry and balance
 - Root node at the center of the screen, child nodes arranged radially around it

Application of Third Dimension

- For large trees, complemented by rotation, translation and zooming
- E.g., **cone trees** child nodes are uniformly radially placed around parent node
 - Primary parameters are radius and translation distance



Arbitrary Graphs/Networks

- Trees are just one category of graphs connected unweighted acyclic graphs
- Other graph representations exist, e.g., graphs with weighted edges, undirected graphs, cyclic graphs, disjoint graphs, ...
- We will focus on arbitrary graphs their structure is not known. Two different approaches:
 - Node-link diagrams
 - Matrix displays

Node-Link Diagrams

- Force-directed graphs strings between nodes
- Links between nodes are iteratively adjusted, until the stress value is minimized
- Example: <u>https://vega.github.io/vega/examples</u> /force-directed-layout/



http://www.absint.com/aisee/gallery.htm

Planar Graphs

- Edges are not intersecting
- Very popular
 - Long history, many studies
 - Edge intersections complicate the interpretation of the graph, it is better to avoid them
 - Sparse according to Euler's formula for n nodes there are at most 3n – 6 edges
- Graphs with intersections can be transformed to planar graphs by introduction of "dummy" nodes at intersection points – after transforming the graph to planar layout, the dummy nodes are removed

Algorithm for Detection of Planarity of Biconnected Graph





Algorithm for Detection of Planarity of Biconnected Graph

- If the graph still contains cycles after the removal of the edges of the outer cycle, it means that one or more pieces contain cycle
- Create subgraph containing this piece and the parts of original cycle containing the endpoints of the piece
- Recursively call the algorithm for detection of planarity



Rendering Planar Graphs

- Visibility approach 2 steps:
 - Visibility step create a representation, where each node is rendered as horizontal segment and each edge as vertical line connecting corresponding segments of the nodes
 - Replacement step each segment corresponding to a node "shrinks" into a point and each vertical connector is replaced by polyline

Rendering Planar Graphs

3





Matrix Representation of Graphs

- Adjacency matrix = grid of NxN dimensions (N is the number of nodes)
 - Binary or containing values of forces or weights of edges
 - Overcomes the problem of edge intersections
 - The strategy for organisation of rows and columns is crucial for revealing interesting patters and structures of the graph

	a	b	С	d	e	f	g	h	
\mathbf{a}			•						
b				•		•			
С	•				•		•	•	
d	•	•				•			
e			•				•	•	
f	•	•		•					
g			•		•			•	
h			•		•		•		

	p	q	r	S	t	u	V	W
p			•					
q	•		•					
r	•	•		•				
S	•	•	•		•			
t				•		•	•	•
u					•		•	•
v					•	•		•
W					•	•	•	

Matrix Representation of Graphs

- Variety of algorithms for row and column reorganisation
 - User driven / automatic
 - Finding the optimal solution is NP-complete problem, therefore the application various heuristics is necessary



en.wikipedia.org

Labelling

- Necessary for understanding what the graph represents
- When rendering trees and graphs the labelling is difficult, because the graphs may contain large amount of nodes and labelling of edges may also be required



Labelling

- For small amount of different labels it is better to use color, size, or shape of the node or color, thickness and the style of the edge line
- If the number of different labels is over 5 or 6 use textual labels
- Small graphs inserted directly into the node (rectangular or oval shape of node) – size of the nodes based on the longest text
- Unified placement of labels for edges:
 - Vertical everything left or everything right to the edge
 - Horizontal everything above or everything below the edge

Labeling

- If the amount of different labels is too large, showing them all at once is not effective. We can use different strategies:
 - Showing labels only in the neighbourhood of current cursor position
 - Various deformations of the visualization, so we can dedicate the given part of the graph larger amount of screen space
 - Rotation of graph in order to reduce overlaps and occlusions of the labels

Labelling





Labeling

- Showing random subset of labels for short time interval and then showing different random subset etc.
- Short-term memory of the user enables remembering of larger amount of labels than when using static view

Labelling

 Ladislav Čmolík, Jiří Bittner, Layout-aware optimization for interactive labelling of 3D models, Computers & Graphics, Volume 34, Issue 4, August 2010, pages 378-387, ISSN 0097-8493

window

lamp

lamp

tire 2

tire 2

front_bumper

body

badge

badge



Trees, Graphs, and Interaction

- Generic types of interaction
 - E.g., trailing camera, zooming
 - Common for all types of visualization
- Specialized interactions
 - E.g., focus + context
 - Applicable for a large variety of visualizations, but primarily developed for visualization of trees and graphs
Interactions with Virtual Camera

- Common interactions (trailing camera, zoom, rotation) that are considered to be simple changes applied to the virtual camera observing a certain part of the scene
- Operations are directed manually or automatically (e.g., flights over the scene, automatic rotation of 3D objects)

Interactions with Graph Elements

- Starts with selection
 - We isolate a single or more graph components
- Graphs with disarranged complicated clusters can be adjusted:
 - Select a set of nodes and drag it to the less cluttered part of the screen
 - Select, translate, or change the shape of edges in order to eliminate their intersections or increase the aesthetical value of the graph
- Problems in dense cluttered regions it is almost impossible to select object unambiguously

Interactions with Graph Structure

- Two basic classes of interaction:
 - Changing the structure of the graph (e.g., reordering the branches of the tree)
 - 2. Focus+context techniques, where a subset of the structure is represented in detail and the rest of the structure just in outline (e.g., fish eye)
 - Performed in screen space
 - Performed in structure space suitable for graphs (enlargement of one branch (see image on the next slide), highlighting of edges adjacent to a given node, ...)

Interactions with Graph Structure





Interactions with Graph Structure

Selective hiding or removal of the selected parts of the graph





vialab.science.uoit.ca

Text and Document Visualization



giladlotan.coms

Definitions

- **Corpus** = set of documents
- We work with objects inside of corpus words, sentences, paragraphs, whole documents, other corpora as well as images and videos
- Texts and documents structured, contain attributes and metadata
- Systems for data mining from documents querying

Levels of Text Representation

- Three levels:
 - Lexical
 - Syntactic
 - Semantic
- Each level requires certain conversion of unstructured text to some form of structured data

Lexical Level

- Transformation of string of characters into sequence of atomic entities = tokens
- Lexical analysers process sequence of characters with a given set of rules into new sequence of tokens
- Tokens contain characters , n-grams, words, lexemes, phrases, ...
- Finite state automata

Syntactic Level

- Identification and annotation of function of each token
- Assignment of marks position of sentence, lexical category, singular or plural, affinity of tokens, ...

Semantic Level

- Extraction of the meaning and the relationship of the findings derived from the structures identified in syntactic level
- Goal is to define analytic interpretation of the whole text in the given context or independent of the context

Vector Space Model (VSM)

- Algebraic model for representation of text documents
- "Term vector" = vector, in which each dimension represent a weight of a given word in a document
- Removal of "stop words" (the, a, ...) for reduction of noise
- Aggregation of words with the same root
- Example of term vector is a hash table which maps unique terms to the number of their occurrences in the document

Vector Space Model

Count-Terms (tokenStream)

- 1.terms := Ø; /* initialize terms
 to empty hash table*/
- 2.for each token t in tokenStream
- 3. do if t is not stop word
- 5.return terms;

Example

• Text example:

There is a great deal of controversy about the safety of genetically engineered foods. Advocates of biotechnology often say that the risks are overblown. "There have been 25,000 trials of genetically modified crops in the world, now, and not a single incident, or anything dangerous in these releases," said a spokesman for Adventa Holdings, a UK biotech firm. During the 2000 presidential campaign, then-candidate George W. Bush said that "study after study has shown no evidence of danger." And Clinton Administration Agriculture Secretary Dan Glickman said that "test after rigorous scientific test" had proven the safety of genetically engineered products.

Example

- The aforementioned paragraph contains 98 string tokens, 74 terms and 48 terms after removal of stop words
- Example of term vector generated by the pseudocode:

genetically	said	safety	engineered	study	test	great	deal	controversy	foods
3	3	2	2	2	2	1	1	1	1

VSM – Computation of Weights

- Various methods of weight assignment, most well known is term frequency inverse document frequency (Tfldf)
- If Tf(w) is term frequency = number of occurrences of a word w in a document, Df(w) is document frequency = number of documents, which contain word w, N is number of documents, then Tfldf(w) is:

$$TfIdf(w) = Tf(w) * \log\left(\frac{N}{Df(w)}\right)$$

VSM – Computation of Weights

 We are interested in words that are frequently occurring in one document but are not so common in other documents of the corpus

id	men	entered	bank	charlotte	missiles	masks	aryan	guns	witnesses	reported	silver	suv	august
seg1.txt	0.239441	0	0.153457	0.195243	0	0.237029	0	0.195243	0.237029	0.140004	0.195243	0.237029	0
seg13.txt	0	0	0	0	0	0	0	0	0	0	0	0	0
seg14.txt	0	0.192197	0	0	0	0	0	0	0	0	0	0	0.172681
seg15.txt	0	0	0	0	0	0	0	0	0	0	0	0	0.149652
seg16.txt	0	0	0	0	0	0	0	0	0	0	0	0	0
seg17.txt	0	0	0	0	0	0	0	0	0	0	0	0	0
seg18.txt	0	0.158432	0	0	0	0	0	0	0	0	0	0	0
seg19.txt	0	0	0	0.197255	0	0	0	0	0	0.141447	0	0	0.155038
seg2.txt	0	0	0	0	0	0	0	0	0	0	0	0	0
seg20.txt	0	0.234323	0	0	0	0	0	0	0	0	0	0	0
seg21.txt	0	0	0	0	0	0	0	0	0	0	0	0	0
seg22.txt	0	0	0	0	0.139629	0	0.127389	0	0	0	0	0	0
seg23.txt	0	0	0	0	0	0	0	0	0	0.180656	0	0	0
seg24.txt	0	0	0	0	0	0	0.117966	0	0	0.117966	0	0	0
seg25.txt	0	0	0	0	0	0	0	0	0	0	0	0	0
seg26.txt	0	0	0	0	0	0	0	0	0	0	0	0	0
seg27.txt	0	0	0.235418	0	0	0	0.214781	0	0	0	0	0	0
seg28.txt	0	0	0	0	0.151753	0	0	0	0	0	0	0	0
seg29.txt	0	0	0	0	0	0	0.129852	0	0	0	0	0	0.142329
seg3.txt	0	0	0	0	0.18432	0	0	0	0	0	0	0	0
seg30.txt	0.078262	0	0	0	0	0	0	0	0	0	0	0	0
seg31.txt	0	0	0.213409	0	0	0	0.194701	0	0	0	0	0	0
seg32.txt	0	0	0	0	0	0	0	0	0	0	0	0	0

Zipf's Law

 In a typical document in a natural language the frequency of any word is inversely proportional to its rank in the frequency table.



• Tag clouds

author biotechnology build concerned contained crops danger detected diet dr earthsave eating engineered extra firm foods found ge genetically incident labeled life monitoring monsanto ph press prevent products proven releases researcher risks rissler safety save sequence shown soybeans stephens study surprised test think trials unfortunately validity vegetarian Wall wild World



 WordTree – tree branches represent various contexts in which the word from the root of the tree occurs in the document – also showing frequency of terms

17 hits

point being that you wouldn't need to know .

safety of genetically engineered -

risks are overblown .

the

, now , and not a single incident , or anything dangerous in these releases , " said a spokesman for adventa holdings , a uk conari press , 2550 ninth st .

- 2000 presidential campaign , then - candidate george w

-case ?

world

-union of concerned scientists , dr .

epa , she is one of the nation's leading authorities on the environmental risks of genetically engineered foods .

foods

products

nation's leading authorities on the environmental risks of genetically engineered foods .

environmental risks of genetically engineered foods .

trials and studies .

wall street journal found that 16 of 20 vegetarian foods labeled as being " free " of genetically engineered products actually contained ge soybeans

validity of all their safety tests ?

author of diet for a new america and founder of earthsave international .





Smith Williams – A History of Science



• Arc Diagrams

-visualizing repeated occurrences in text

• Bach's minuet in G dur:



• Literature Fingerprints



Visualization of Set of Documents

- The goal is to place similar documents close to each other and different documents far apart
- Algorithm computes the similarity between all pairs of documents and this then drives their placement – O(n²) complexity

Visualization of Set of Documents

- Self-Organizing Maps machine learning algorithm. Collection of 2D nodes, into which we place the documents. Each node contains vector of the same dimensionality as the input vectors of the training documents
- At the beginning initialize the SOM nodes typically randomly. Select random vector, compute its distance from the other nodes. Assign weights to the closest nodes (within given radius) – the closest node has the largest weight. Iterate over input vectors while decreasing the radius.

Self-Organizing Maps



Self-Organizing Maps - Example

vaku	utusala	lipponen	tulva
donner			
	Lundh	0101	
moottoritie	esiopet	usuudistus	tulos
nah,jan	sttk	pörss.	i -
		kana	nattavuus
kone et.a		pomni	
raubanpalkinto 98	iku		hanko
1		wäktner	64.3
olvi			lakko
linnainmaa alho	kausi		
	kärkö1	ässä työvä	enpuolue.
keittiö		elisabe	•
lovilsa	khat	.emi	muotokuva
mainonta	sche	open	lamminen
States of the second			
työttömyys creu	tzfeldt		albright
karhu	si	φ.	
konea			jeltsin
tah	allaan	niinistö	and the second second

Visualization of Set of Documents

- Themescapes summary information about corpora in the form of 3D terrains
- Height and color used for representation of density of similar documents



Extended Methods for Text Visualization

- Include also metadata:
 - Software Visualization
 - Search Result Visualization
 - Temporal Document Collection Visualizations
 - Representing Relationships

Software Visualization



Search Result Visualization

- TileBars each document of the result set is represented by rectangle where width indicates relative length of the document and layered squares inside correspond to text segments. The darker the square the higher the frequency of the queried set of terms
- Compact representation and information about the structure of the document reflecting relative length of the document, frequency of the queried terms and their distribution

Search Result Visualization



Example



Temporal Document Collection Visualizations

 ThemeRiver – visualization of thematic changes in time for a set of documents, vertical thickness corresponds to frequency in the given time



Representing Relationships

Jigsaw List view

